

Bayesian Networks Workshop

Brescia, 18 5 2015

On Bayesian networks and information quality (InfoQ)

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Joint work with Silvia Salini, Federica Cugnata and Galit Shmueli



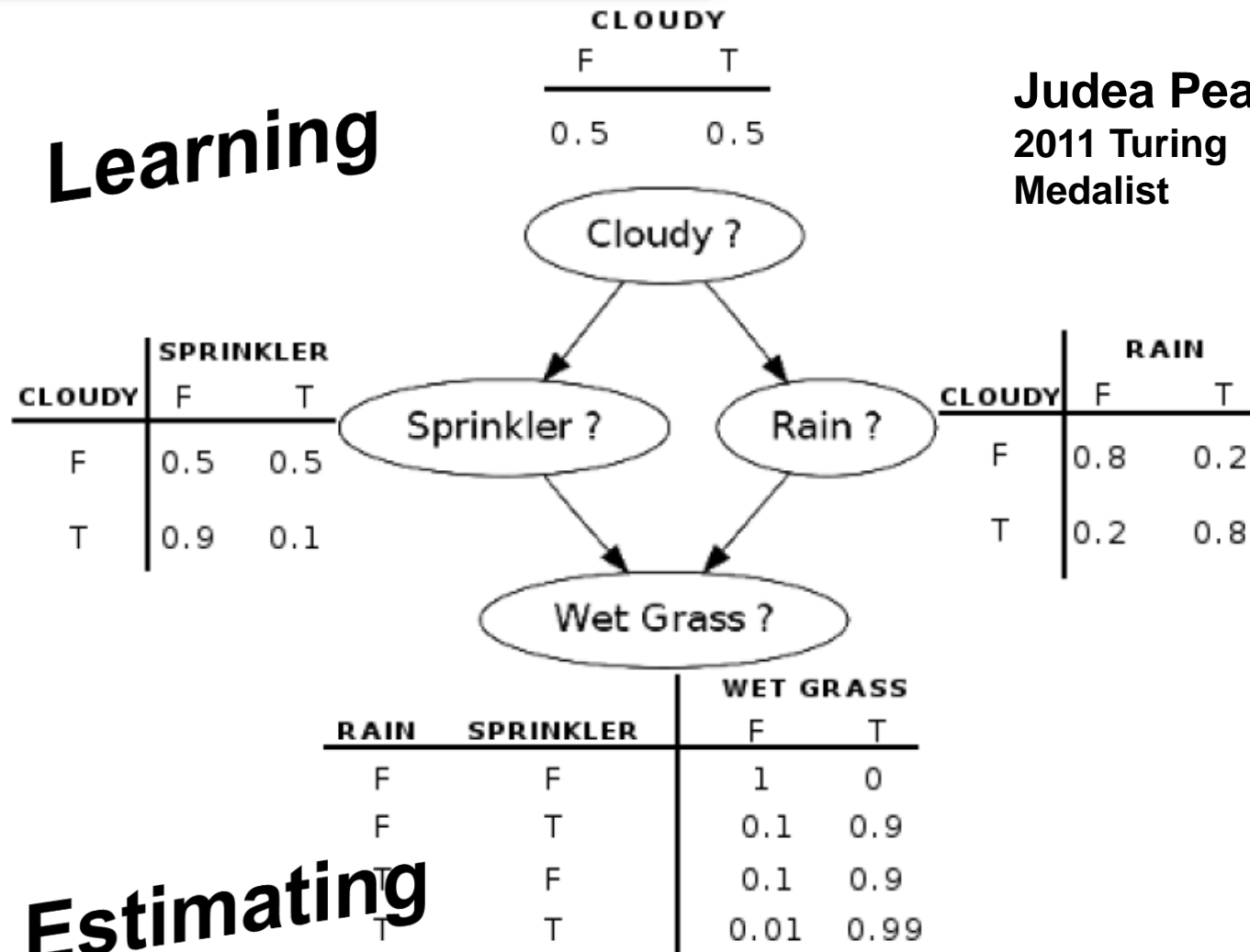
Applied statistics is about
meeting the challenge of
**solving real world
problems**
with **mathematical tools**
and **statistical thinking**

"Much fine work in statistics involves minimal mathematics; some bad work in statistics gets by because of its apparent mathematical content."

David Cox (1981),
Theory and general principle in statistics, *JRSS(A)*, 144, pp. 289-297.

Why Bayesian Networks?

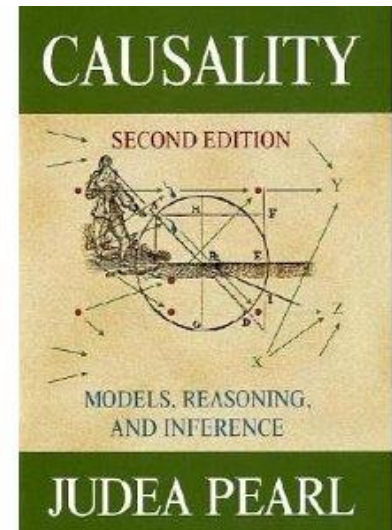
Learning



Judea Pearl
2011 Turing
Medalist



Estimating



W. Edwards Deming (1900-1993)

“Tests of variables that affect a process are useful only if they **predict what will happen if this or that variable is increased or decreased.**

Statistical theory, as taught in the books, is valid and leads to operationally verifiable tests and criteria for an **enumerative study**. Not so with an **analytic problem**, as the conditions of the experiment will not be duplicated in the next trial.

Unfortunately, most problems in industry are analytic.”*



*From preface to *The Economic Control of Quality of Manufactured product* by W. Shewhart, 1931

“Statistics is important because it is conceived as contributing to a **causal understanding** ...

Statistics can indicate causality *even in the absence of a mechanistic understanding.*

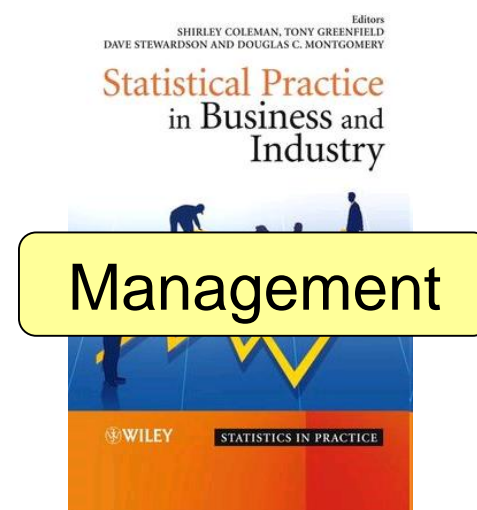
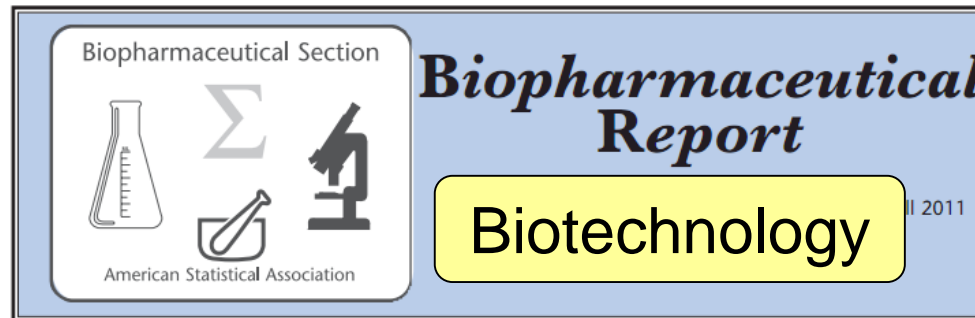
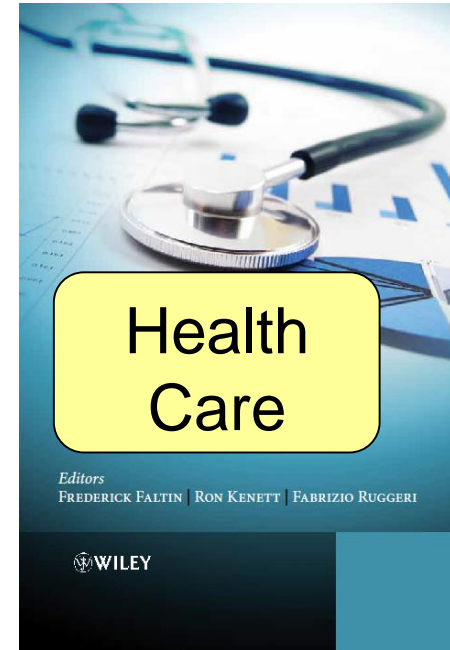
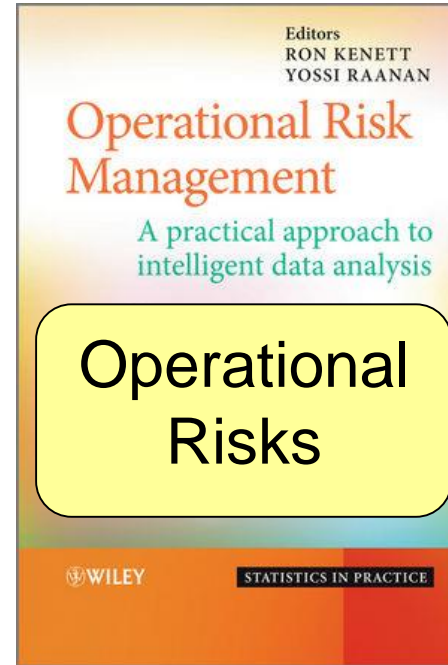
But the traditional self-conception of statistics is that it can rarely say anything about causality.

This is a ***paradox.***”



*Statistikk 50 År! Some remarks on causality**

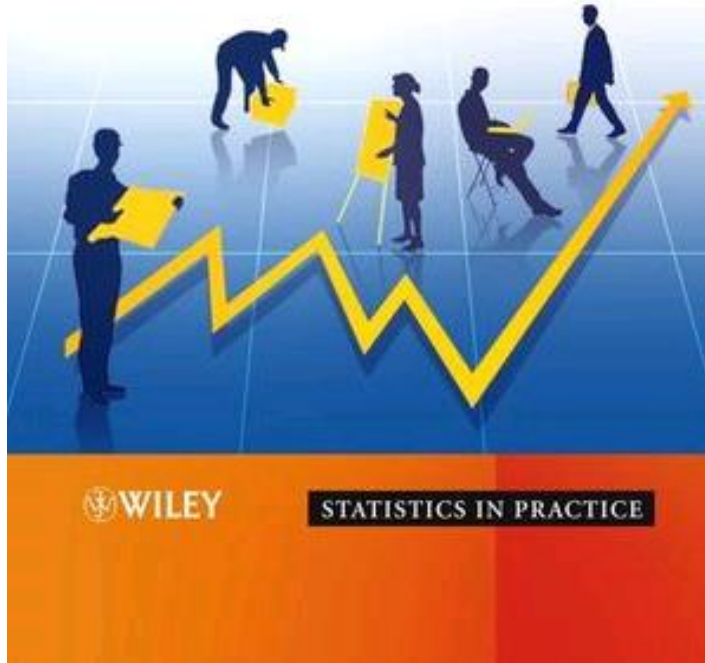
Odd O. Aalen



The 7 case studies

Editors
SHIRLEY COLEMAN, TONY GREENFIELD
DAVE STEWARDSON AND DOUGLAS C. MONTGOMERY

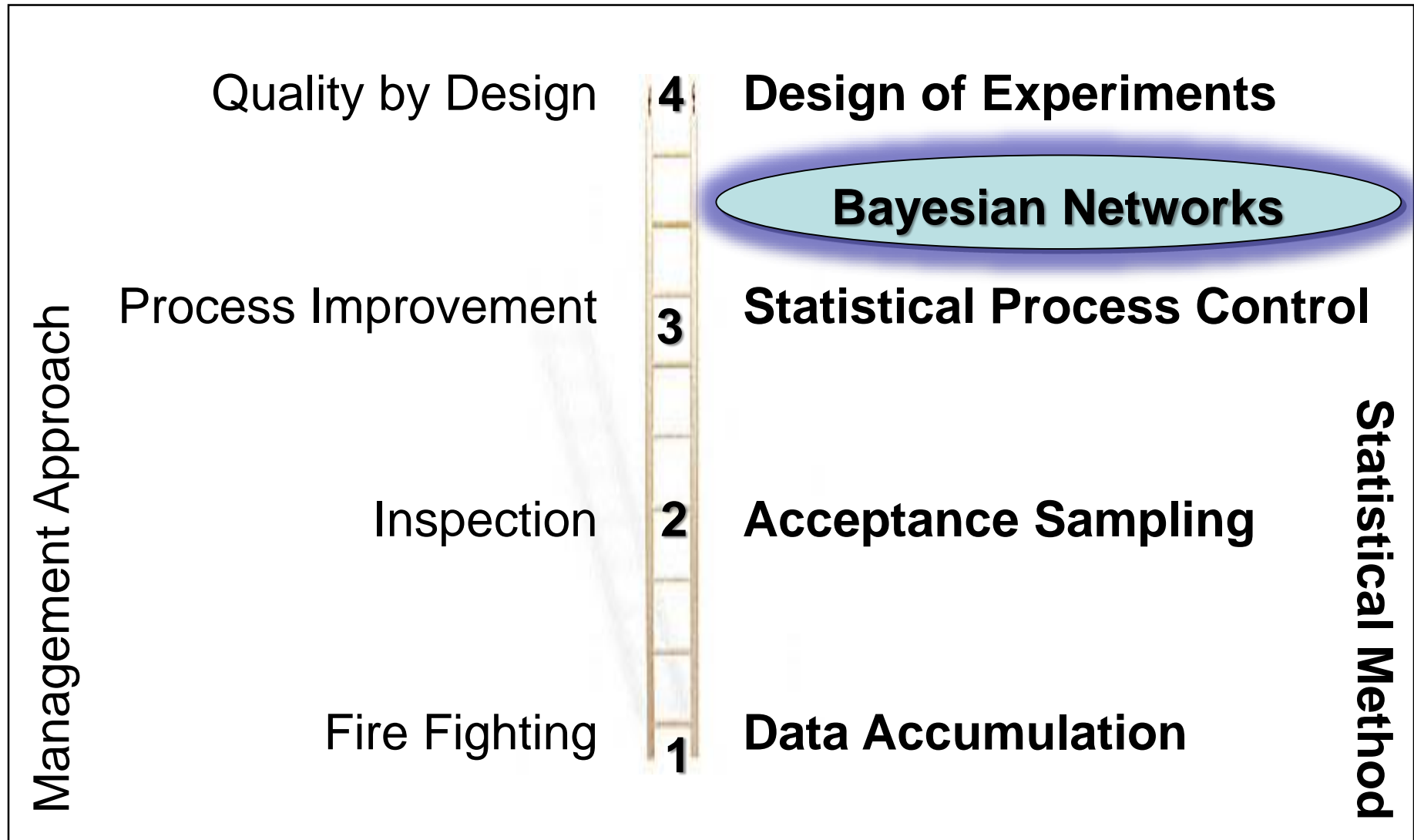
Statistical Practice in Business and Industry



Management

Conjecture Validation

The Quality Ladder



PSE=Practical Statistical Efficiency

$$\mathbf{PSE} = \mathbf{E}\{\mathbf{R}\} \times \mathbf{T}\{\mathbf{I}\} \times \mathbf{P}\{\mathbf{I}\} \times \mathbf{V}\{\mathbf{PS}\} \times \mathbf{P}\{\mathbf{S}\} \times \mathbf{V}\{\mathbf{P}\} \times \mathbf{V}\{\mathbf{M}\} \times \mathbf{V}\{\mathbf{D}\}$$

PSE component: 1-5

“1”= not very good, “5” = excellent.

Impact

$\mathbf{V}\{\mathbf{D}\}$ = Value of the **D**ata actually collected

$\mathbf{V}\{\mathbf{M}\}$ = Value of the statistical **M**ethod employed

$\mathbf{V}\{\mathbf{P}\}$ = Value of the **P**roblem to be solved

$\mathbf{P}\{\mathbf{S}\}$ = **P**robability that the problem actually gets **S**olved

$\mathbf{V}\{\mathbf{PS}\}$ = Value of the **P**roblem being **S**olved

$\mathbf{P}\{\mathbf{I}\}$ = **P**robability the solution is actually **I**mplemented

$\mathbf{T}\{\mathbf{I}\}$ = **T**ime the solution stays **I**mplemented

$\mathbf{E}\{\mathbf{R}\}$ = **E**xpected number of **R**eplications

L=Maturity Level on Quality Ladder: 1- 4

1 = Fire fighting (FF), 2 = Inspection (I),

3 = Process Improvement (PI), 4 = Quality by Design (QbD)

Maturity

The Statistical Efficiency Conjecture

Let $PSE = PSE$ of a specific project.

PSE is a random variable with specific realisations for individual projects, $1 \leq PSE \leq 5^8$.

$E\{PSE\}$ = The expected value of PSE in a given organisation over all projects.

The Statistical Efficiency Conjecture is linking Expected Practical Statistical Efficiency with the maturity of an organisation on the Quality Ladder.

In more formal terms it is stated as:

Conjecture:

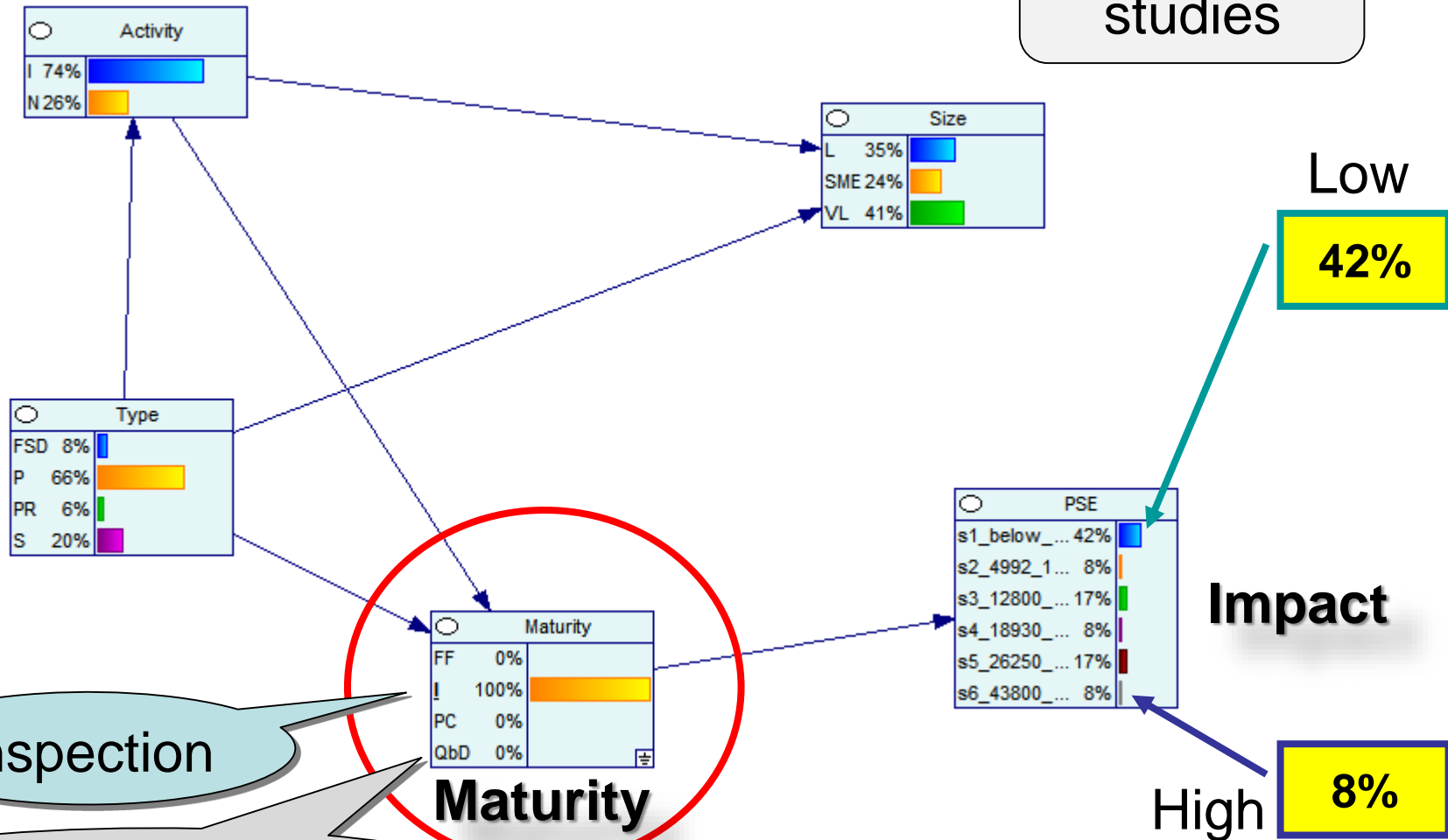
Conditioned on the right variable,

$E\{PSE\}$ is an increasing function of L

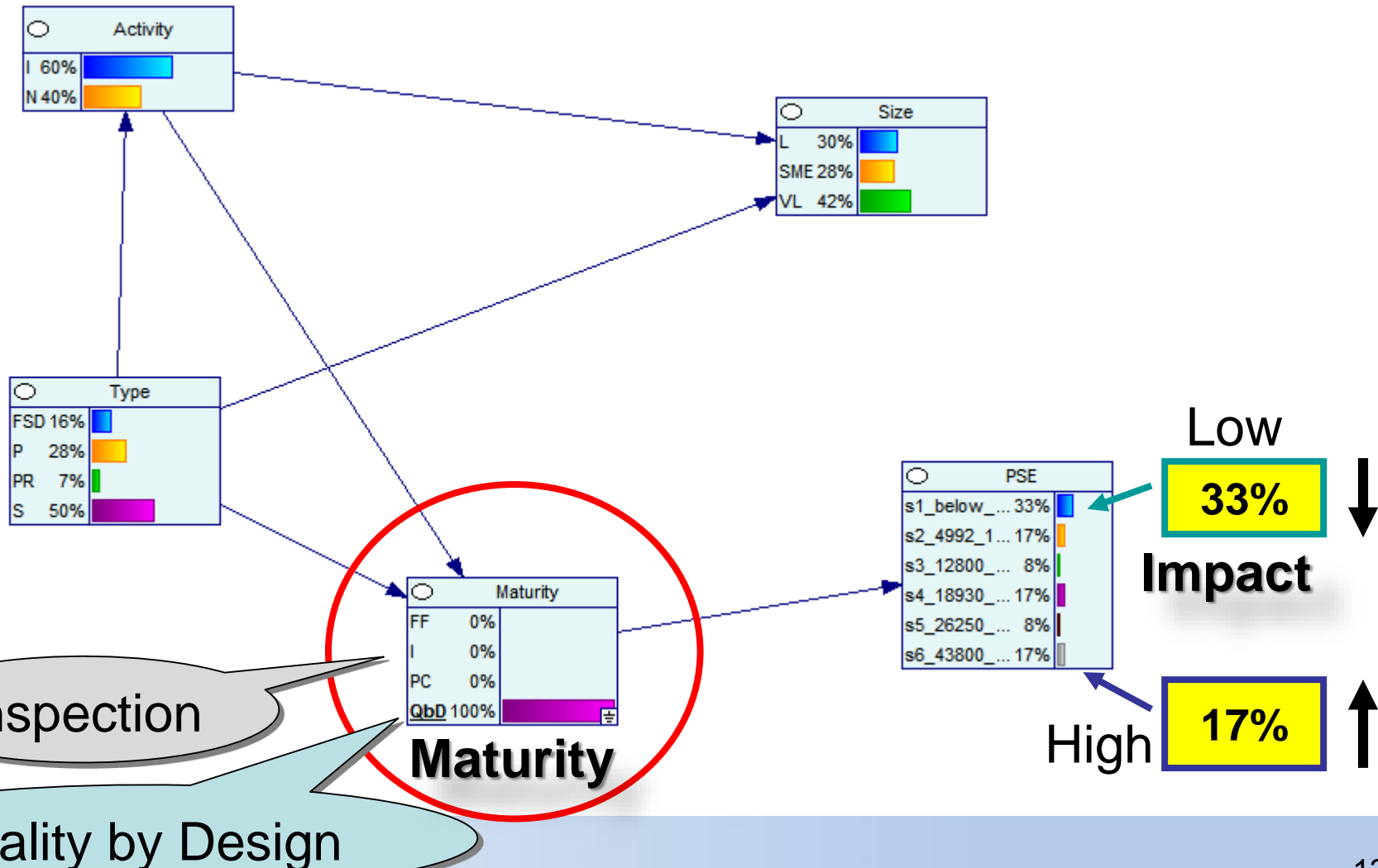


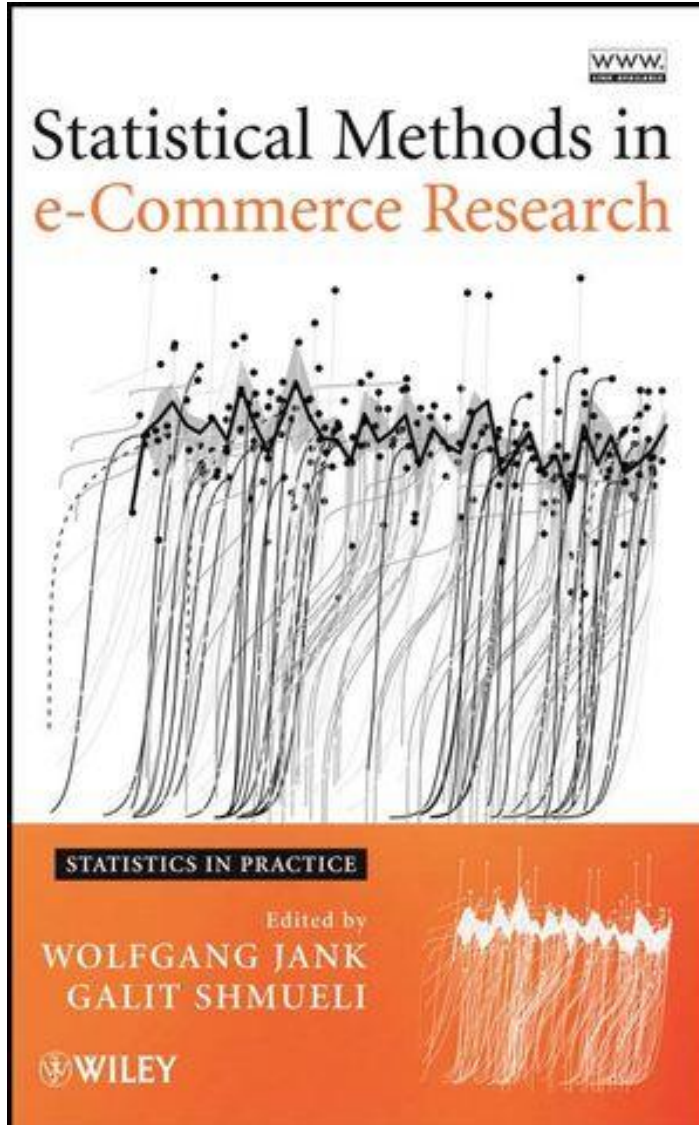
The Statistical Efficiency Conjecture

21 case studies



The Statistical Efficiency Conjecture





Web Usability

Usability Monitoring

Case study 2

The Seven Layers of a *Decision Support for User Interface Design* (DSUID)

The lowest layer – user activity

The second layer – page hit attributes (data)

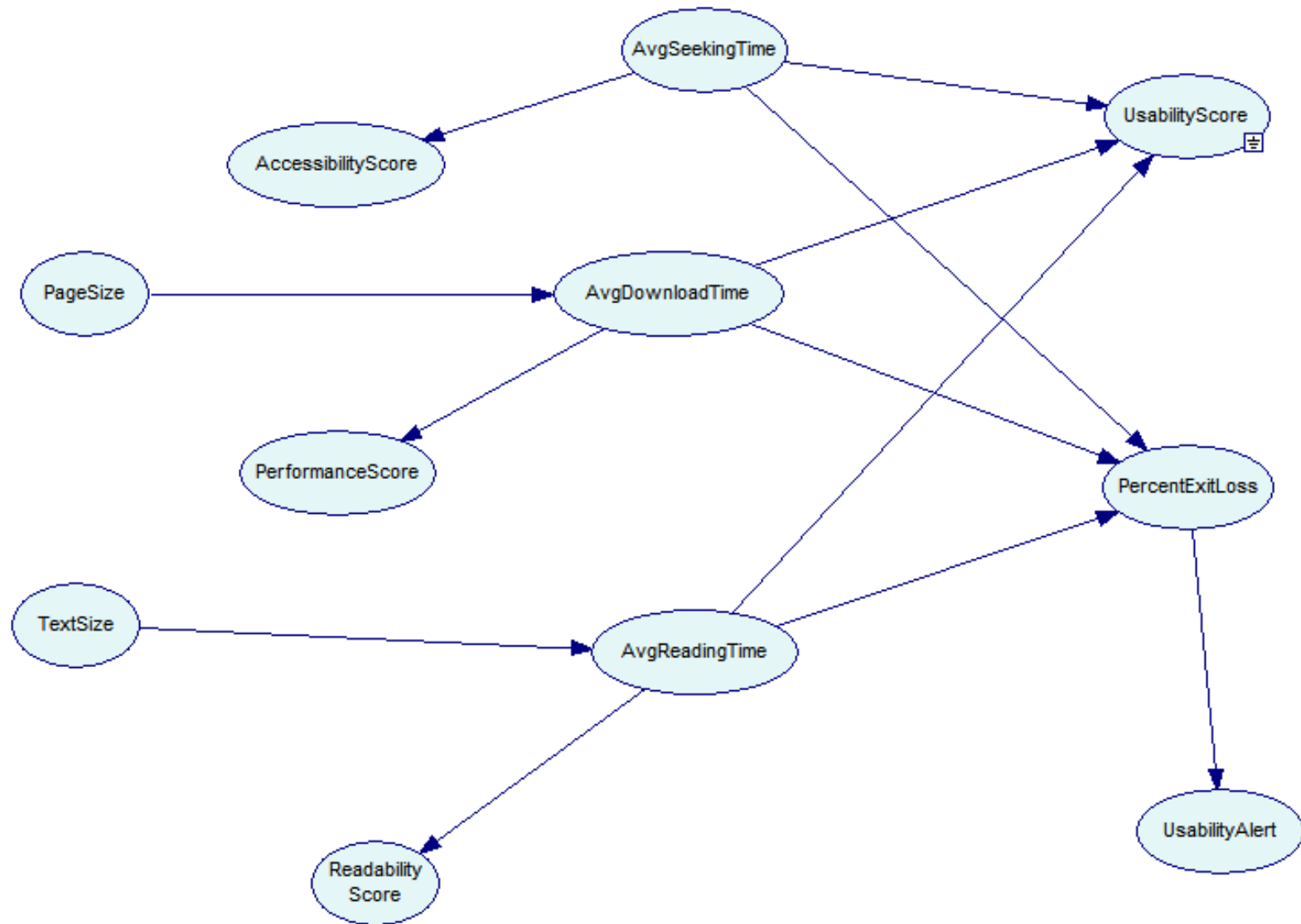
The third layer – transition analysis (dynamic)

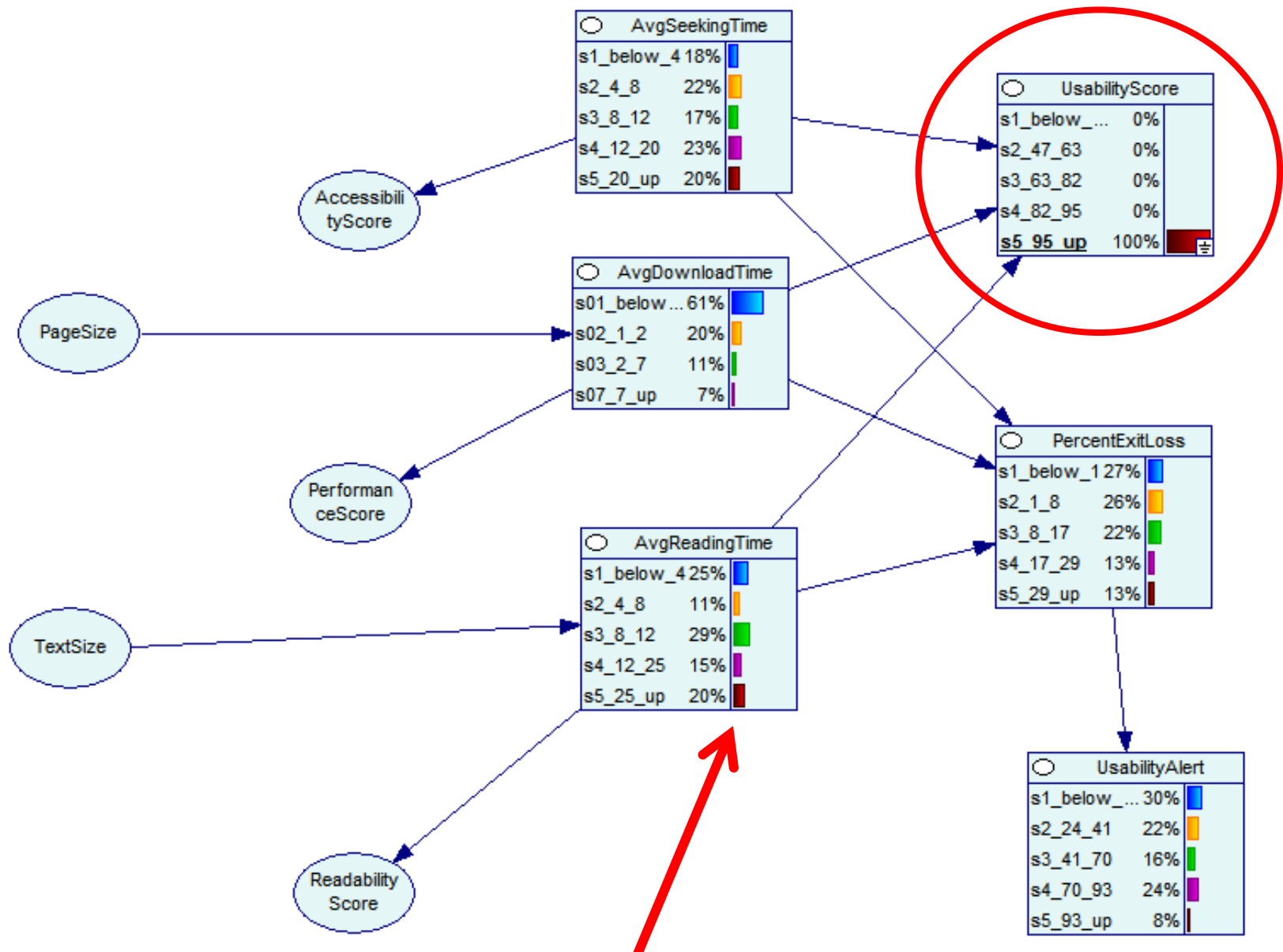
The fourth layer – UPI identification (quant.  subjective)

The fifth layer – usage statistics (descriptive)

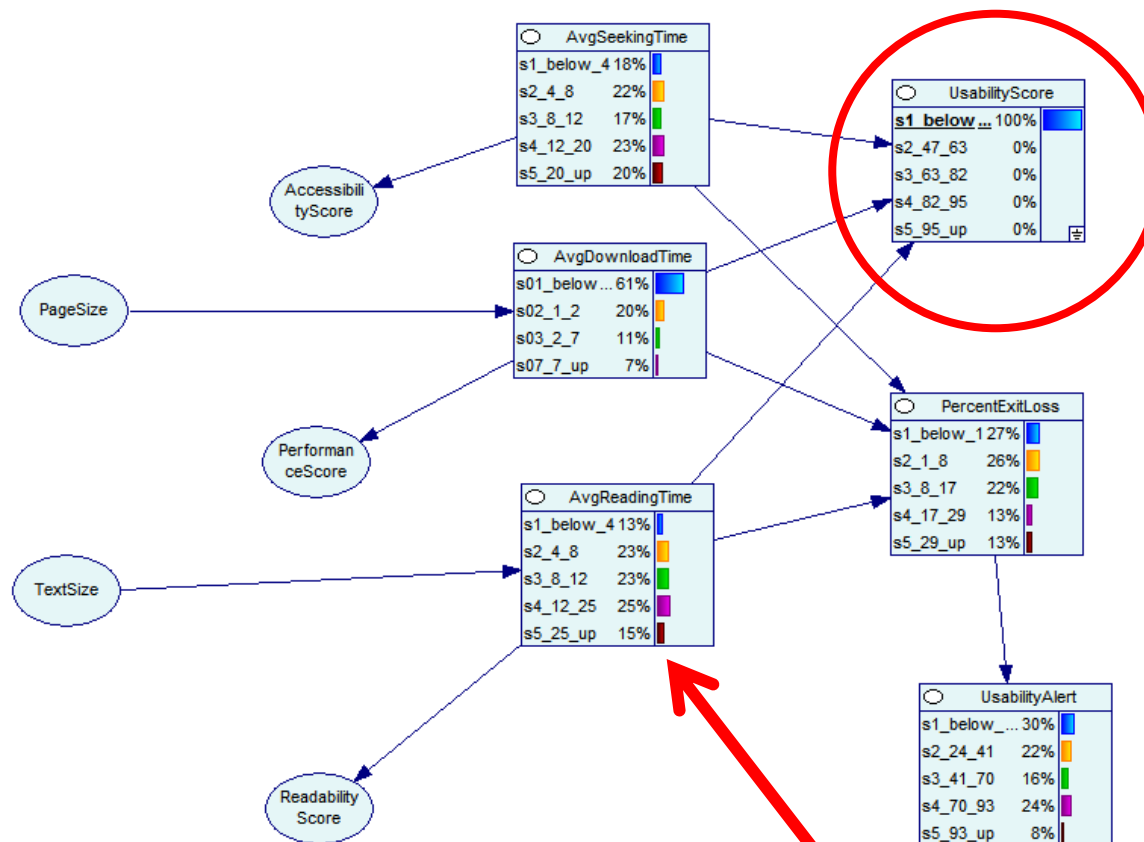
The sixth layer – statistical decision (t-test, BN,...)

The top layer – interpretation

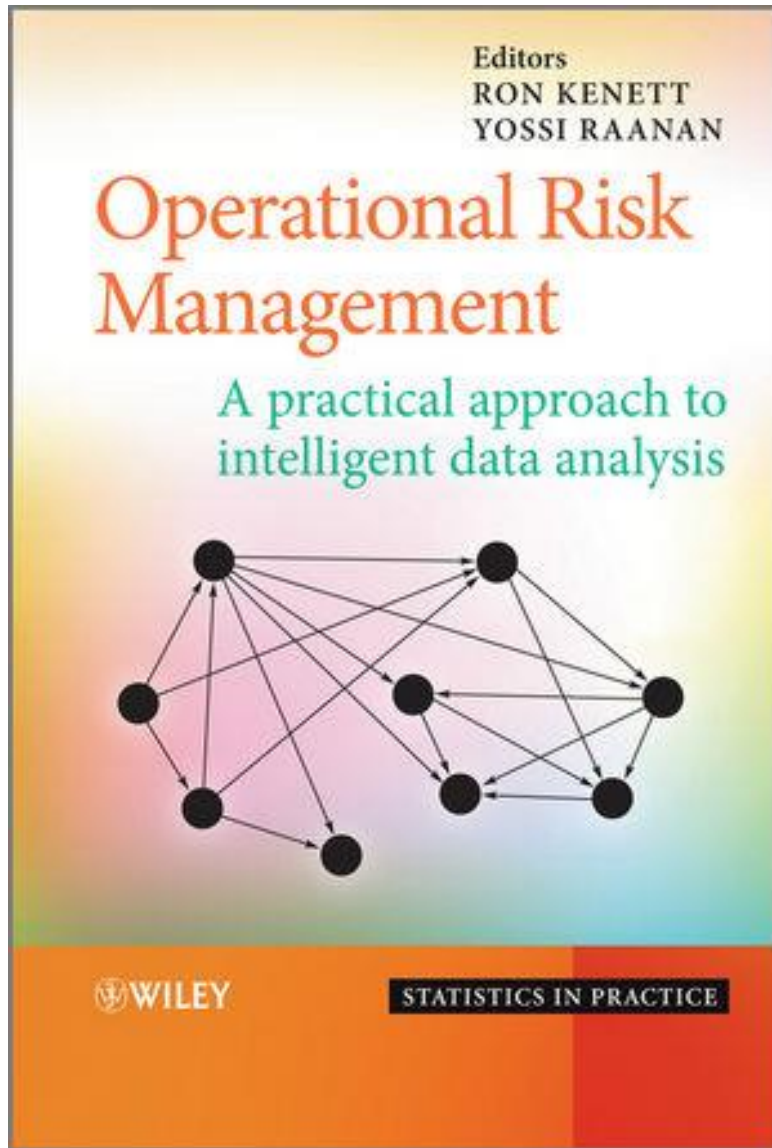




20% high reading time ➡ high usability



Lower high reading time (drop to 15% from 20%) ➡ low usability



Operational Risks

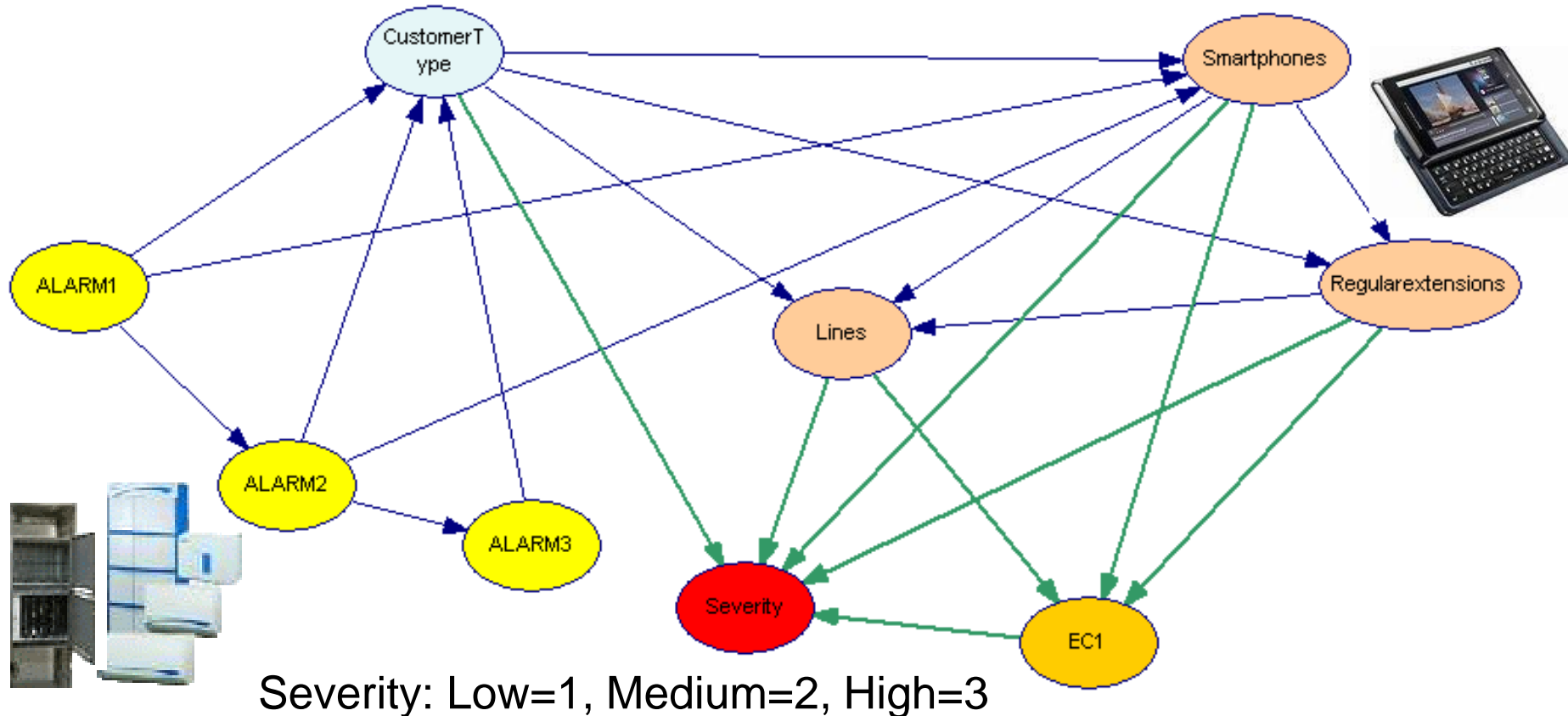
Predictive Application

Case study 3

A: Lines - 4 levels for lines

B: Extensions - 5 levels for regular extension

C: Smart phones - 6 levels for smart phones



Statistics from the empirical GoF distribution

Run number	Lines	Extensions	Smart phones	GoF mean	GoF Std	5th%	95th%
1	1	1	1	56.60941	0.059105706	56.62155	57
2	1	1	2	59.63072	0.02490878	59.62382	59.88322
3	1	1	3	61.82233	0	61.82233	61.82233
4	1	1	4	61.58676	0.003056467	61.58734	61.66847
5	1	1	5	61.58476	0.002951751	61.58734	61.66847
6	1	1	6	61.82233	0	61.82233	61.82233
7	1	2	1	57.39454	0.048655559	57.39338	57.75812
8	1	2	2	58.16235	0.043181378	58.16356	58.48932
9	1	2	3	61.82233	0	61.82233	61.82233
10	1	2	4	60.37945	0.018637201	60.38212	60.58919
11	1				0	61.82233	61.82233
12	1				0	61.82233	61.82233
13	1				0.0002	55.29014	55.76737
14	1				0.0002	58.88973	59.20304
15	1				0	61.82233	61.82233
16	1				0	61.82233	61.82233
17	1				0	61.82233	61.82233
18	1				0	61.82233	61.82233
19	1				0.5877	54.76769	55.22726
20	1				0.1381	57.38467	57.76721
21	1				0	61.82233	61.82233
22	1				0	61.82233	61.82233
23	1				0.6506	61.58734	61.66847
24	1				0.3469	61.58734	61.67658
25	1	5	1	61.58135	0.002950407	61.57922	61.66847
26	1	5	2	61.58483	0.003111372	61.57922	61.67658
27	1	5	3	61.5814	0.002882963	61.57922	61.66847
28	1	5	4	61.58221	0.003007665	61.58734	61.66847
29	1	5	5	61.58598	0.002768952	61.58734	61.66847
30	1	5	6	61.82233	0	61.82233	61.82233
31	2	1	1	58.63324	0.037792725	58.63446	58.95804
32	2	1	2	58.39079	0.042223195	58.39521	58.7367
33	2	1	3	59.87708	0.025846298	59.87487	60.11655
34	2	1	4	55.81579	0.065592685	55.80323	56.25833
35	2	1	5	61.82233	0	61.82233	61.82233

Robustness of Prediction

From a given BN one can generate simulated outcomes. Goodness of fit (GoF) of a BN model is computed using a distance measure between simulated data and the real data

Classification error

$$\sum_{i=1}^{runs} I_{(s_i \neq \ddot{s}_i)}(x)$$

Indicator function of the subset of severities, s , of the set X

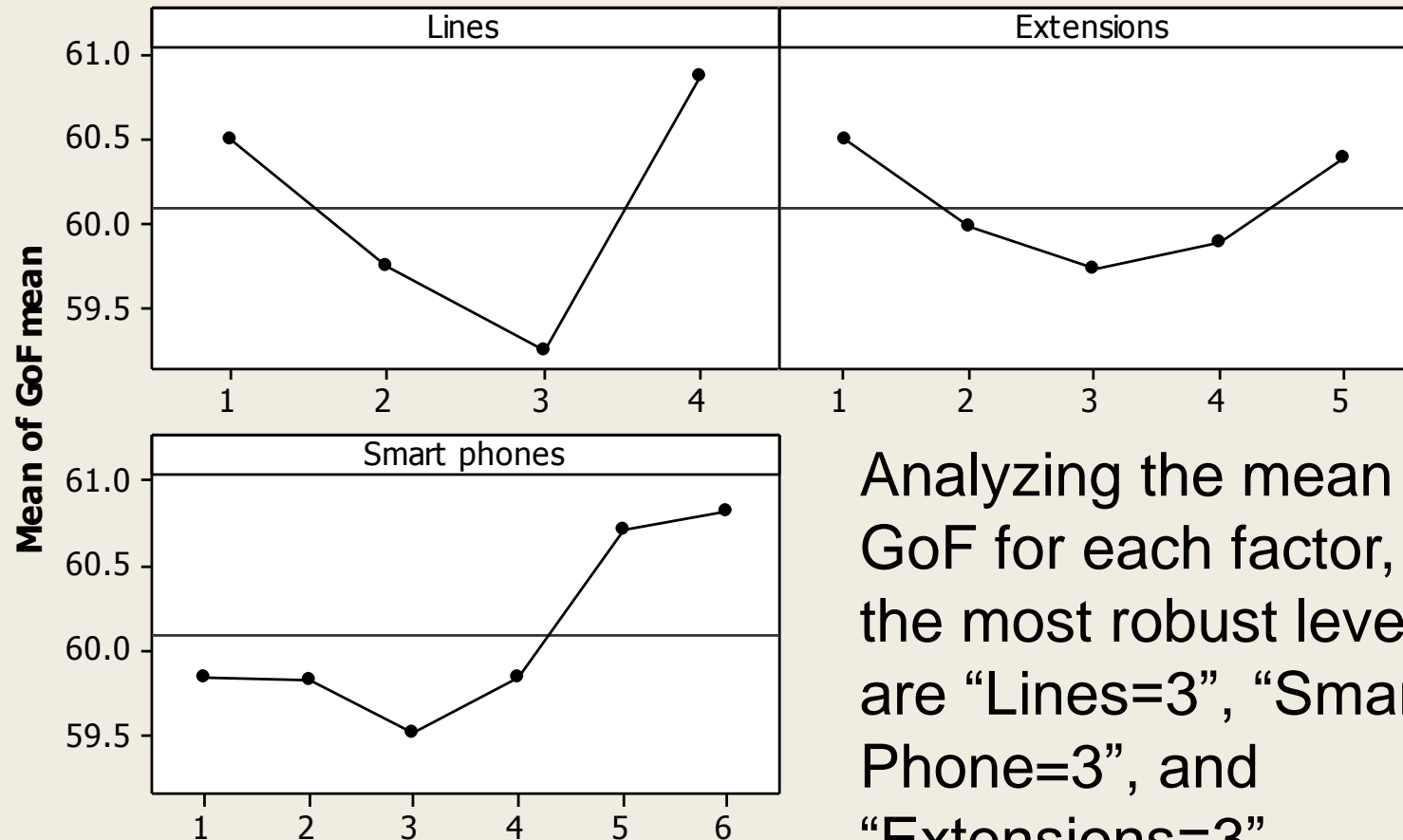
$$I = \begin{cases} 1 & \text{if } x \in \{s : s_i \neq \ddot{s}_i\} \\ 0 & \text{if } x \notin \{s : s_i \neq \ddot{s}_i\} \end{cases}$$

S_i the real data

\ddot{s}_i the i-th simulated values of severity

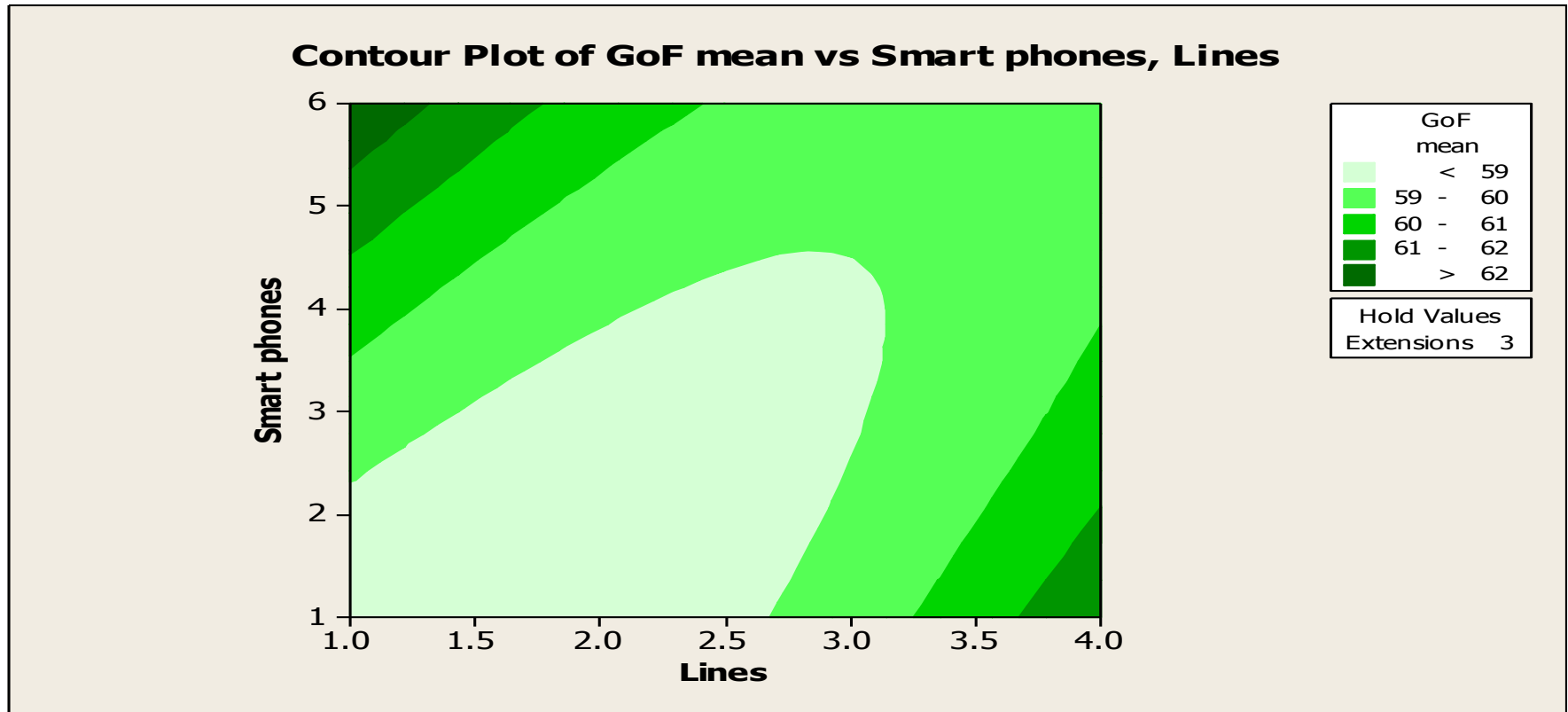
Analysis: Main effect plots of mean GoF

Main Effects Plot (data means) for GoF mean

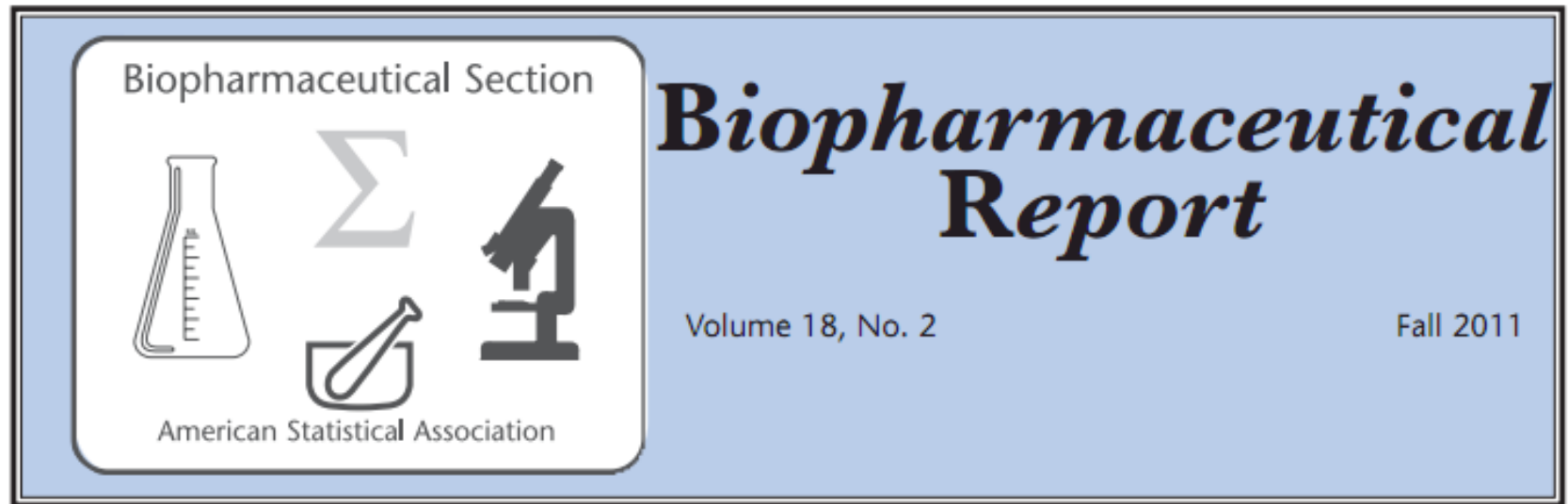


Analyzing the mean GoF for each factor, the most robust levels are “Lines=3”, “Smart Phone=3”, and “Extensions=3”

Analysis: Interaction plots of mean GoF



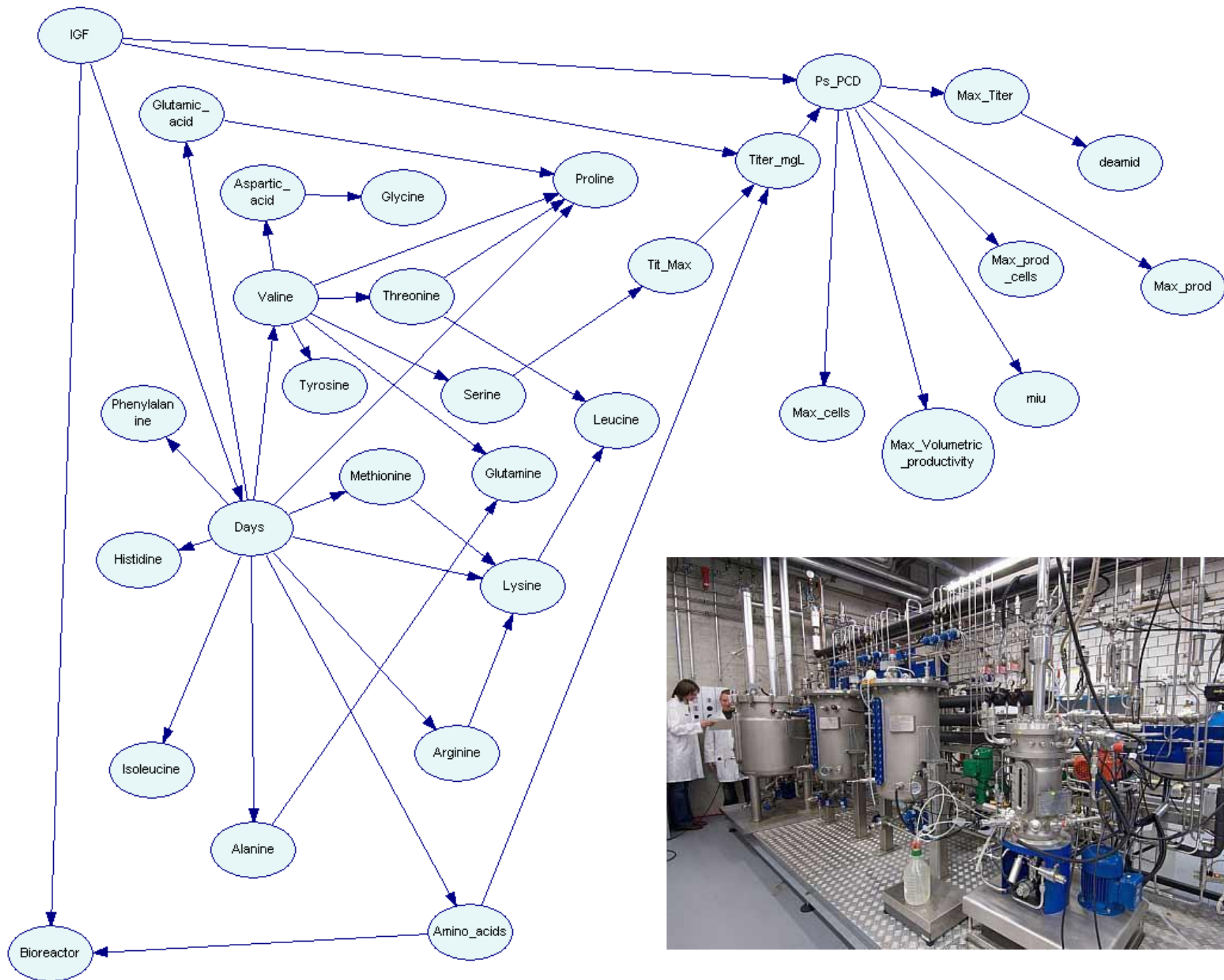
A limited number of lines and a limited level for smart phone is associated with a low mean GoF

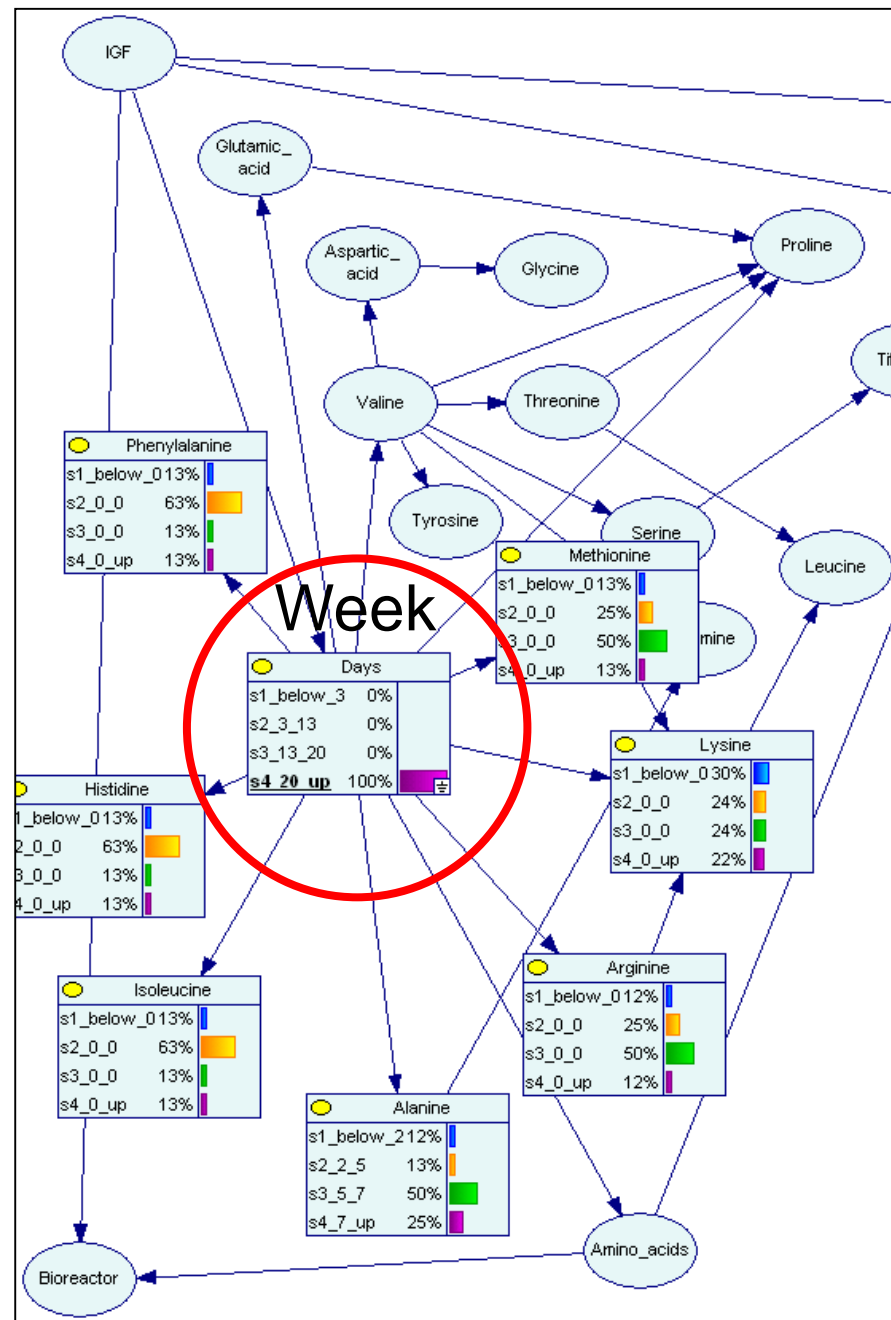
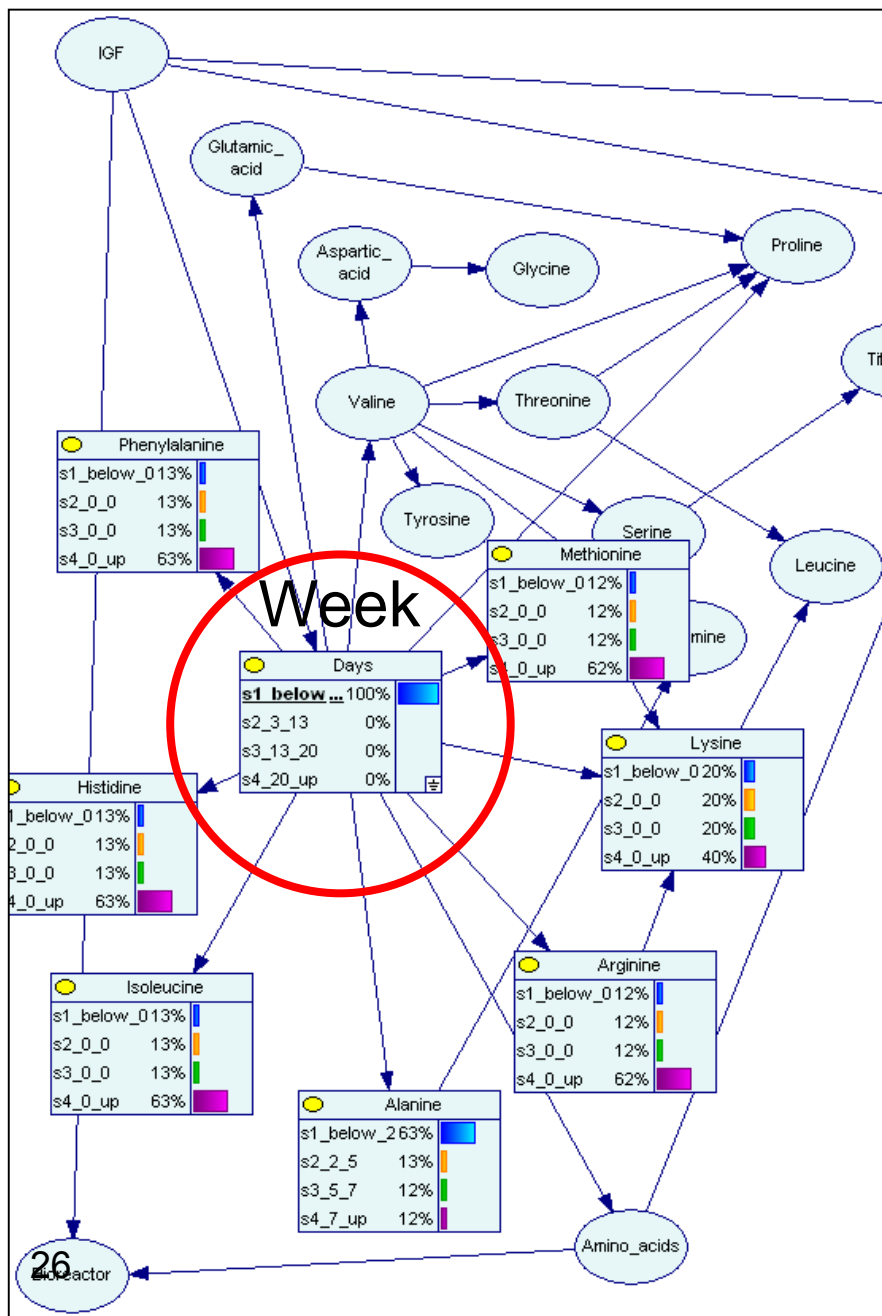


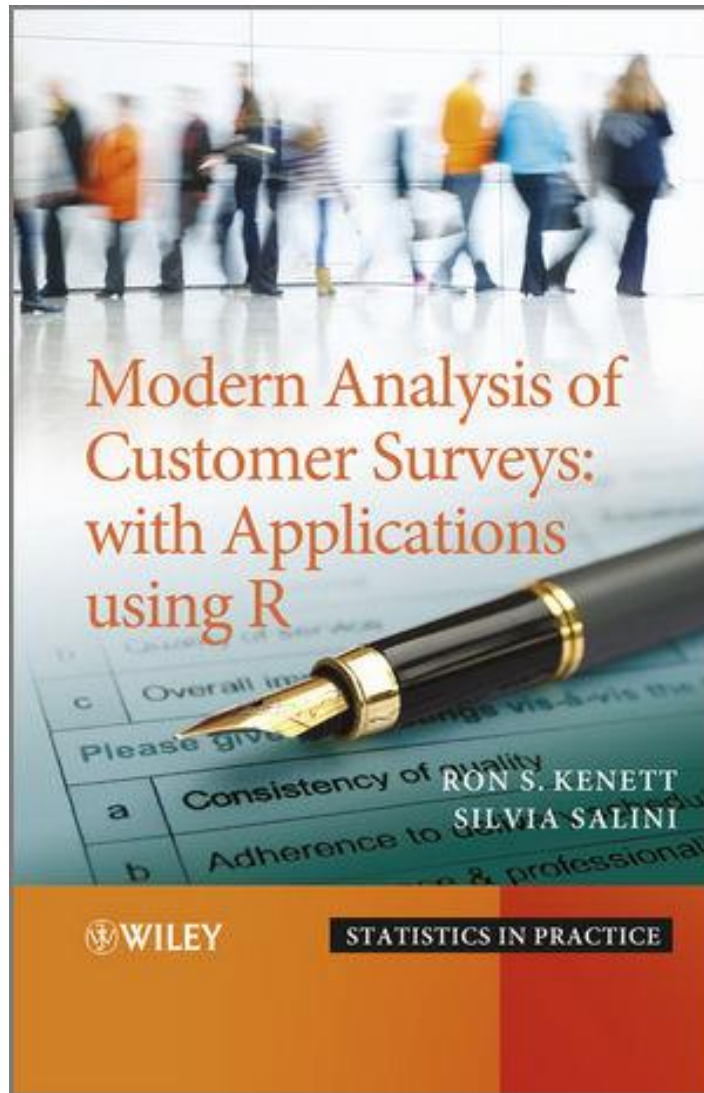
Biotechnology

Modeling Effect of Time

Case study 4







Customer Surveys

Diagnostic Application

The ABC 2010 Annual Customer Satisfaction Survey

Company: _____

Completed by: _____

Title/Position: 1. Owner 2. Management 3. Technical Management 4. Technical Sta
5. Operator 6. Administrator 7. Other, please specify: _____

Dear Customer,

For each of the following statements, please select a number indicating the extent of your agreement with the statement concerning your experience with ABC during 2010. Then, under "Importance Level", select another number indicating the importance of the statement to you. If a certain statement is not relevant or not applicable, please select N/A.

Overall Satisfaction from ABC

	<u>Evaluation</u>				
	Very low				Very high
1. Overall satisfaction level from ABC:	1	2	3	4	5
2. Overall satisfaction level from ABC's improvements during 2010:	1	2	3	4	5
3. Is ABC your best supplier?	a. Yes b. No				
4. Would you recommend ABC to other companies?	Very unlikely 1	2	3	4	Very likely 5
5. If you were in the market to buy a PRODUCT, how likely would it be for you to purchase an ABC product again?	1	2	3	4	5

Equipment and System

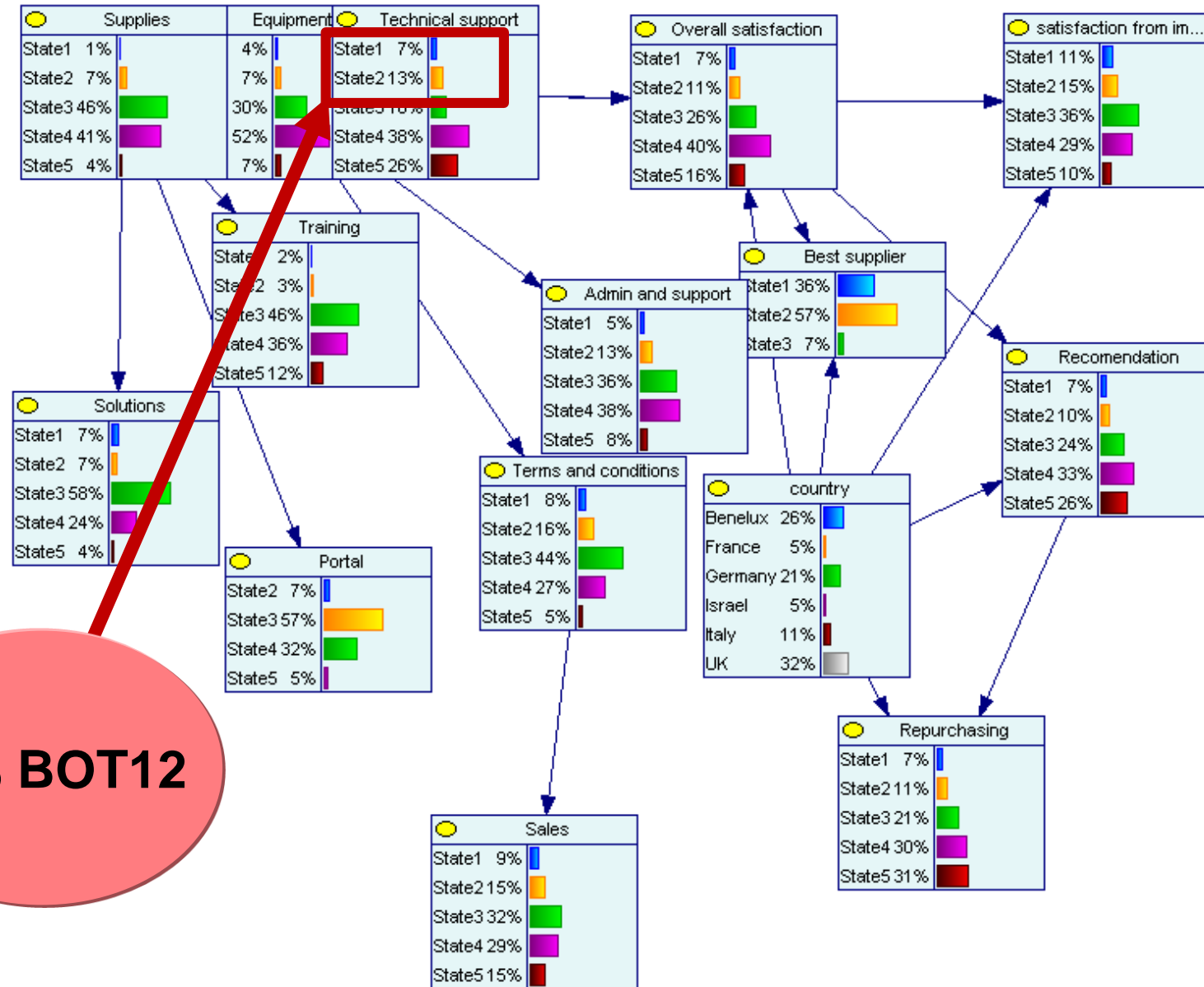
	<u>Evaluation</u>					<u>Importance Level</u>			
	Strongly disagree				Strongly agree	Low		High	
6. The equipment's features and capabilities meet your needs.	1	2	3	4	5	1	2	3	N/A
7. Improvements and upgrades provide value.	1	2	3	4	5	1	2	3	N/A
8. Output quality meets or exceeds expectations.	1	2	3	4	5	1	2	3	N/A
9. Uptime is acceptable.	1	2	3	4	5	1	2	3	N/A
10. For customers who purchased a system during 2010: ABC's equipment proposal met your requirements.	1	2	3	4	5	1	2	3	N/A
11. Overall satisfaction level from the equipment :	Very low 1	2	3	4	Very high 5				

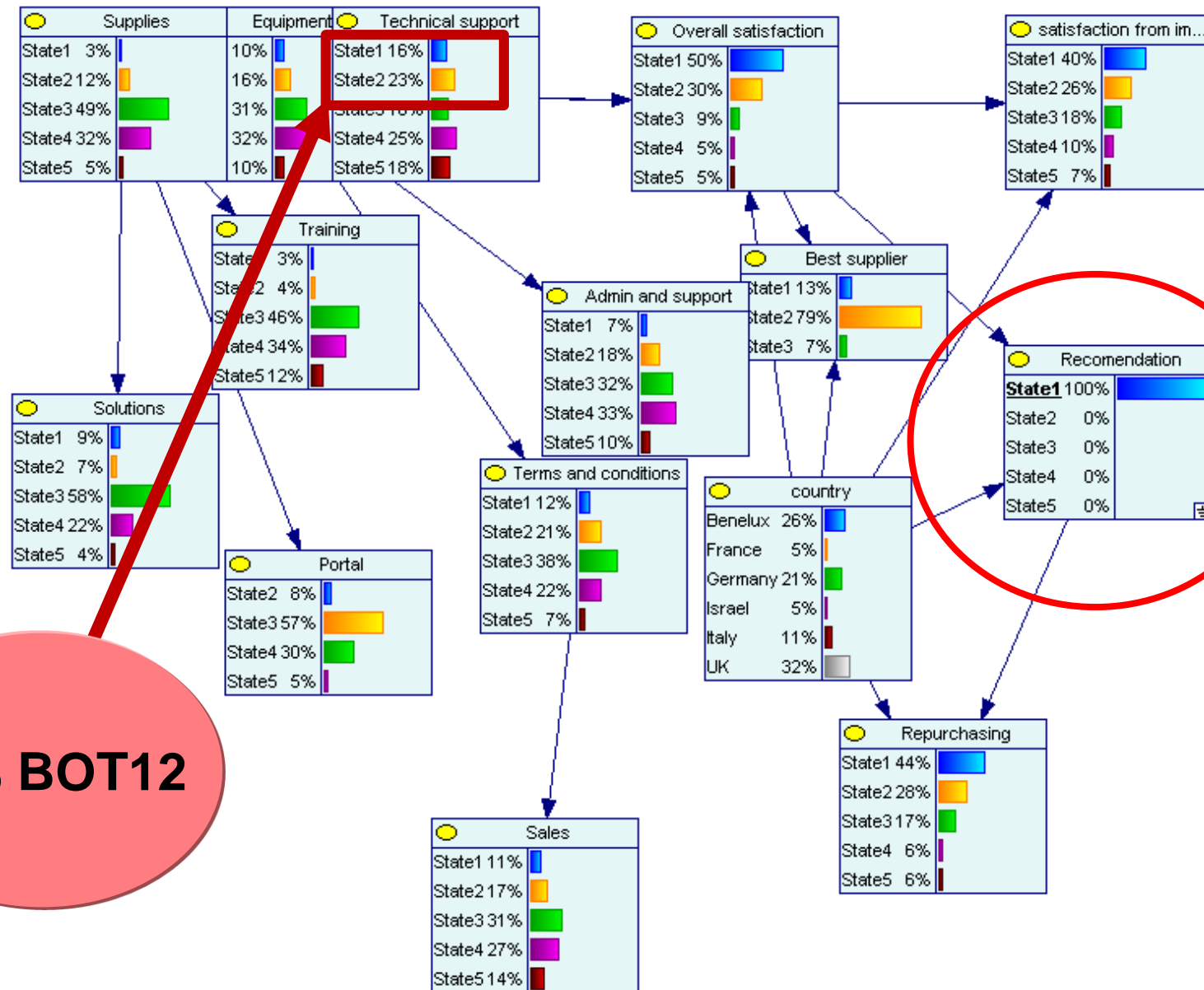
Sales Support

	<u>Evaluation</u>					<u>Importance Level</u>			
	Strongly disagree				Strongly agree	Low		High	
12. Verbal promises have been honored.	1	2	3	4	5	1	2	3	N/A
13. Sales personnel communicate frequently enough with you.	1	2	3	4	5	1	2	3	N/A
14. Sales personnel respond promptly to requests.	1	2	3	4	5	1	2	3	N/A
15. Sales personnel are knowledgeable about equipment.	1	2	3	4	5	1	2	3	N/A
16. Sales personnel are knowledgeable about market opportunities.	1	2	3	4	5	1	2	3	N/A
17. Overall satisfaction level from sales support :	Very low 1	2	3	4	Very high 5				

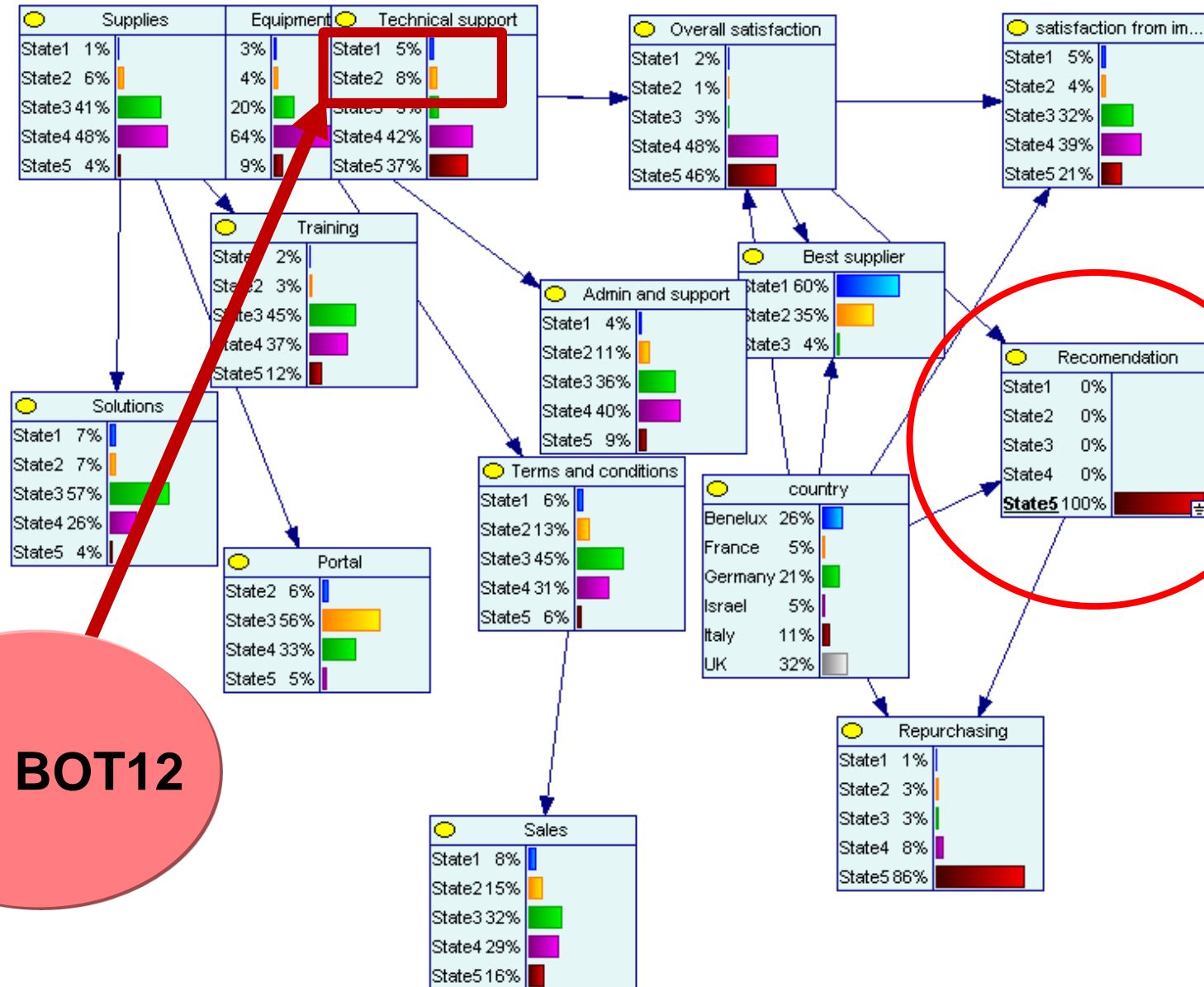
Technical Support

	<u>Evaluation</u>					<u>Importance Level</u>			
	Strongly disagree				Strongly agree	Low		High	
18. Technical support is available when needed.	1	2	3	4	5	1	2	3	N/A
19. The technical staff is knowledgeable.	1	2	3	4	5	1	2	3	N/A
20. The technical staff is well informed about the latest equipment updates/enhancements.	1	2	3	4	5	1	2	3	N/A
21. Parts are available when needed.	1	2	3	4	5	1	2	3	N/A
22. The remote support care center is valuable and meets your expectations.	1	2	3	4	5	1	2	3	N/A
23. Problems are resolved within the required time frame.	1	2	3	4	5	1	2	3	N/A
24. The technical staff is courteous and helpful.	1	2	3	4	5	1	2	3	N/A
25. Overall satisfaction level from technical support :	Very low 1	2	3	4	Very high 5				





39% BOT12

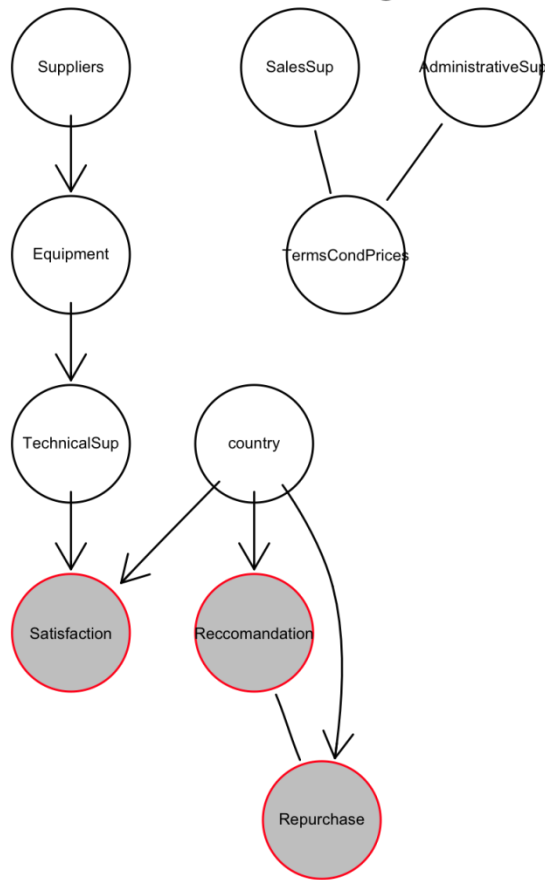


13% BOT12

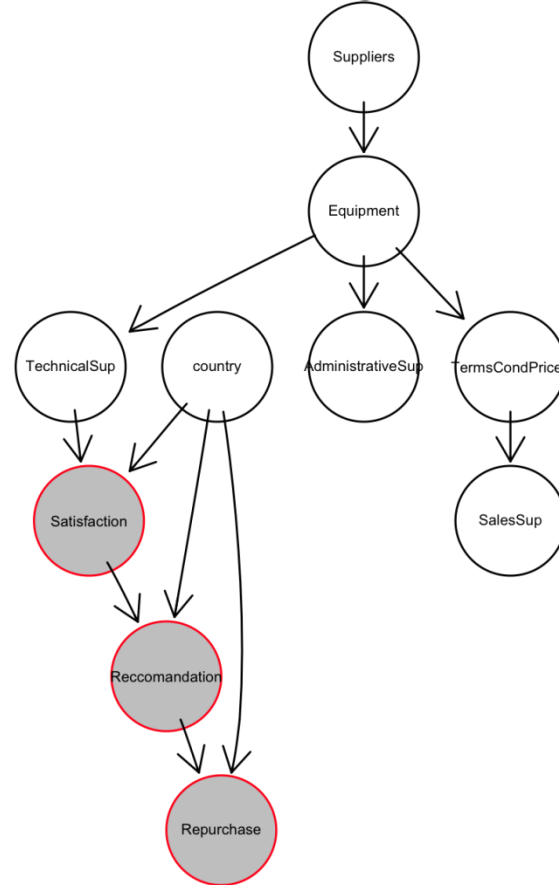
Network learning

Robustness of Network

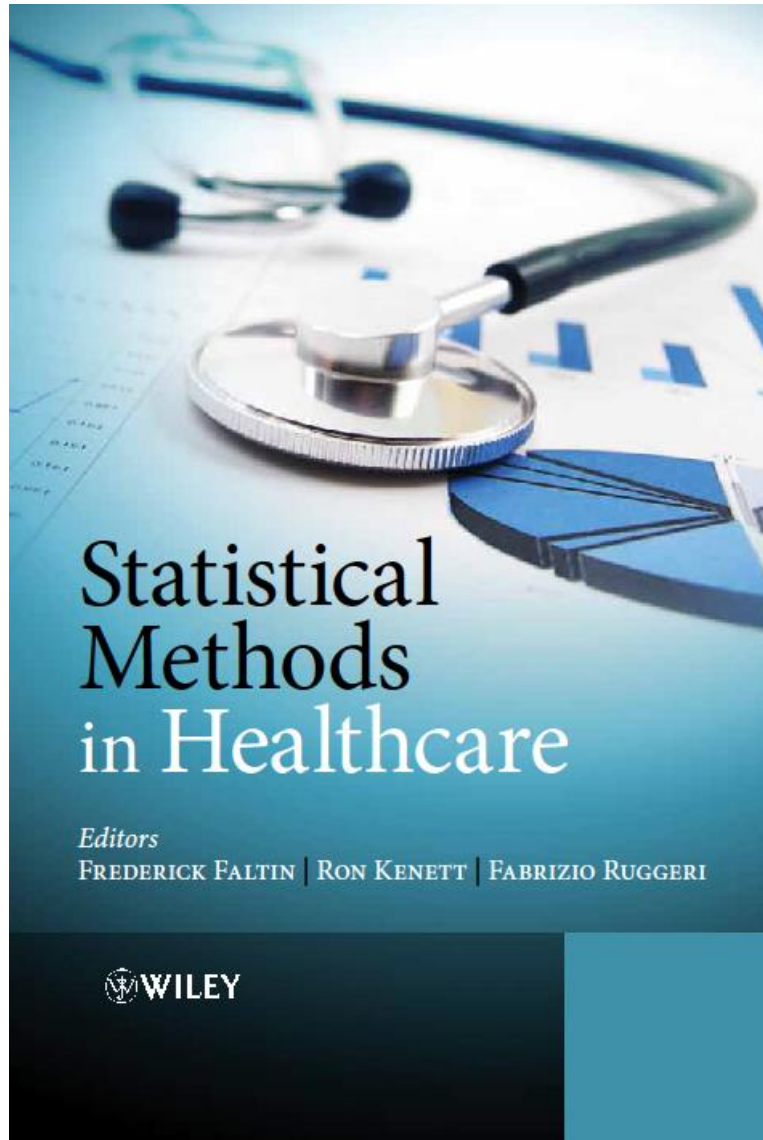
Constraint-based algorithms



Scored-based algorithms



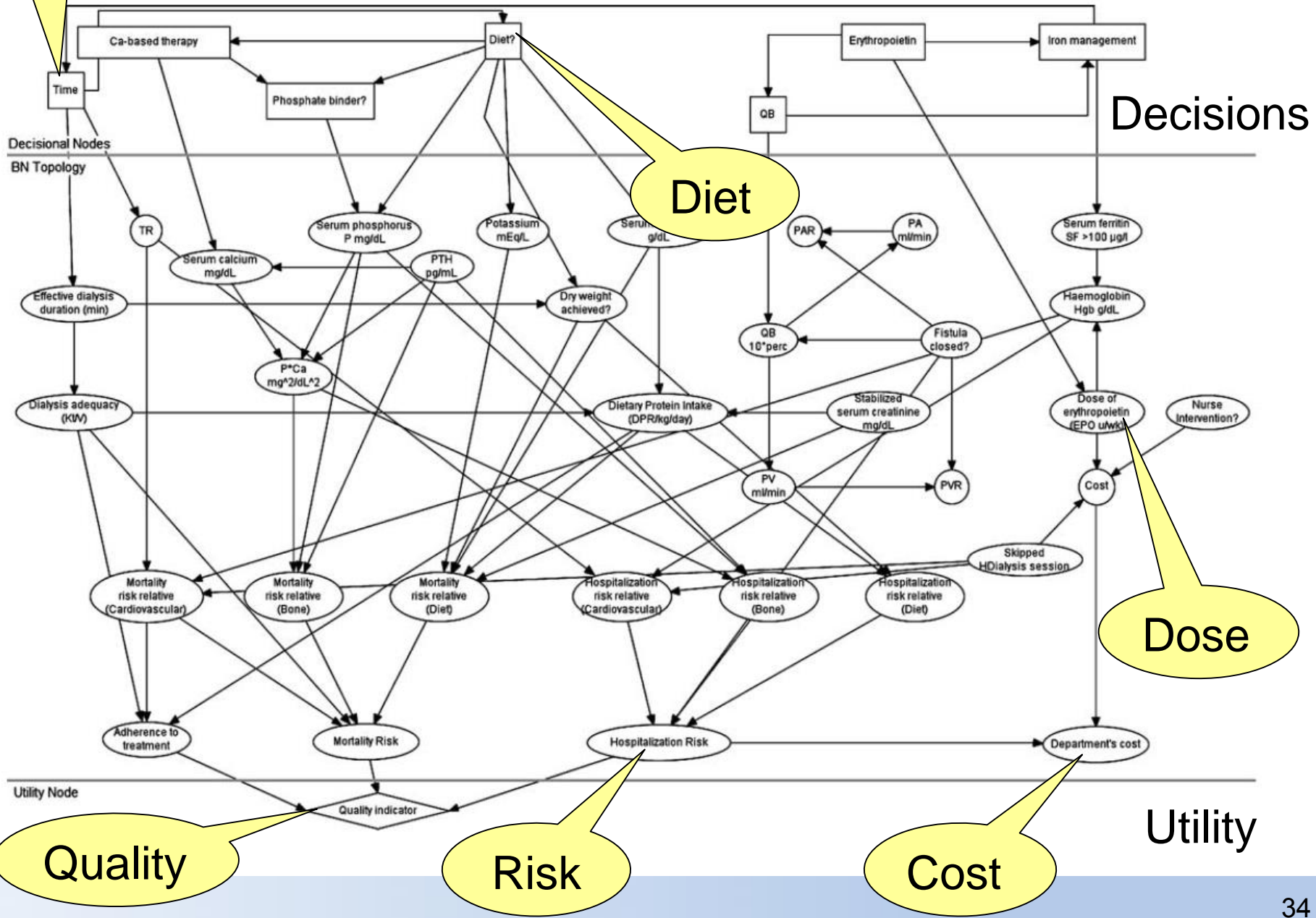
bnlearn: 1) Grow-Shrink (GS) algorithm, 2) Incremental Association (IAMB) algorithm, 3) Interleaved-IAMB (Inter-IAMB) algorithm, 4) Fast-IAMB (Fast-IAMB) algorithm, 5) Max-Min Parents and Children (MMPC) algorithm, 6) ARACNE and Chow-Liu algorithms, 7) Hill-Climbing (HC) greedy search algorithm, 8) Tabu Search (TABU) algorithm, 9) Max-Min Hill-Climbing (MMHC) algorithm and 10) two-stage Restricted Maximization (RSMAX2) algorithm for both discrete and Gaussian networks



Health Care

Decision Support Systems

Time

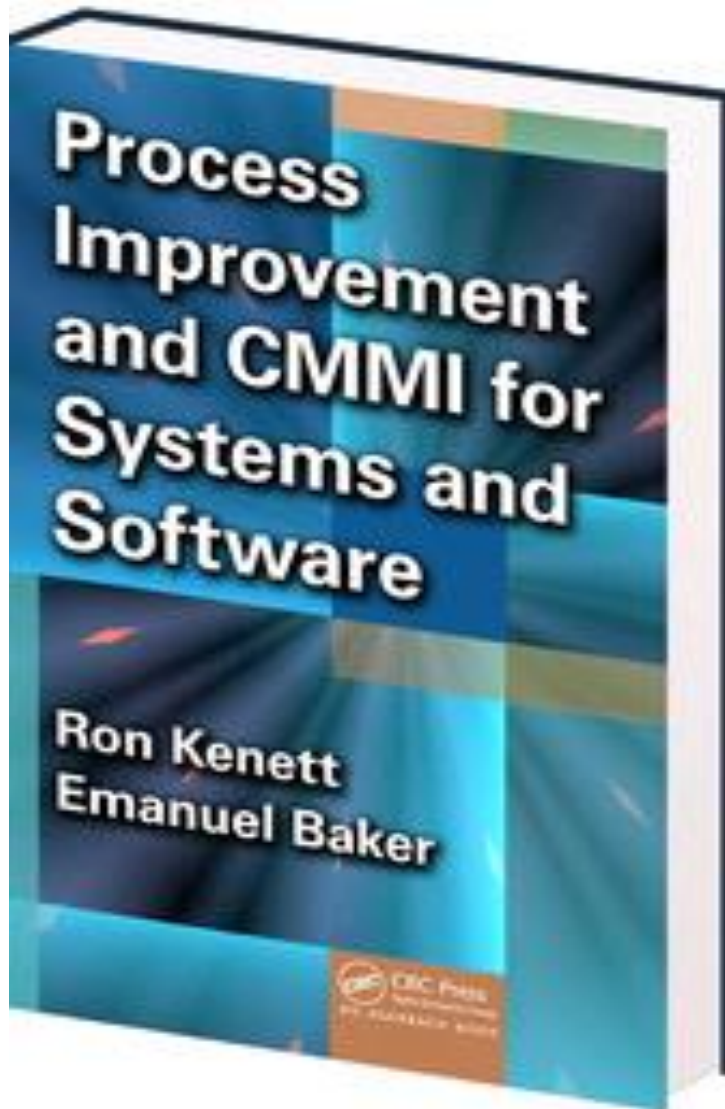


Risk

Decision	State of Actions
Ca-based Therapy	<ul style="list-style-type: none"> * Treat hypercalcemia; * Continue current therapy; * Decrease vitamin D dose to achieve ideal Ca; Decrease Ca-based ... * Decrease or discontinue vitamin D dose or Ca-based phosphate binders; ...
Phosphate binder?	<ul style="list-style-type: none"> * Assess nutrition, discontinue phosphate binder if ... * Being dietary counseling and restrict dietary phosphate; start or increase ... * Being short-term Al-based phosphate binder use, then increase ...
QB	<ul style="list-style-type: none"> * Increase QB; * Keep QB; * Decrease QB.
Erythropoietin	<ul style="list-style-type: none"> * Keep the current dose; ...
Iron Management	<ul style="list-style-type: none"> * Keep the treatment; ...
Time	...
Diet?	...

Pt. 2	Pt. 5
Hospitalization Ratio 1.0E-3 0 - 1.5 0.00 1.5 - 3 35.54 3 - 4.5 58.64 4.5 - 6 5.46 6 - 7.5 0.31 7.5 - 9	Hospitalization Ratio 1.0E-3 0 - 1.5 0.00 1.5 - 3 28.86 3 - 4.5 63.74 4.5 - 6 6.99 6 - 7.5 0.35 7.5 - 9
Mortality Ratio 4.82 0 - 3 43.74 3 - 6 16.19 6 - 9 21.02 9 - 12 5.43 12 - 15 3.95 15 - 18 2.38 18 - 21 1.23 21 - 24	Mortality Ratio 9.71 0 - 3 30.65 3 - 6 19.54 6 - 9 14.02 9 - 12 11.59 12 - 15 8.91 15 - 18 4.10 18 - 21 0.87 21 - 24
Mortality risk relative (Ca) 14.04 0 - 1 85.58 1 - 1.5 0.38 1.5 - 2 1.0E-3 2 - 2.5 1.0E-3 2.5 - 3 1.0E-3 3 - 3.5 1.0E-3 3.5 - 6	Mortality risk relative (Ca) 4.91 0 - 1 93.19 1 - 1.5 1.90 1.5 - 2 1.0E-3 2 - 2.5 1.0E-3 2.5 - 3 1.0E-3 3 - 3.5 1.0E-3 3.5 - 6
Mortality risk relative (B...) 18.00 0 - 1 78.68 1 - 1.5 0.59 1.5 - 2 1.0E-3 2 - 2.5 1.0E-3 2.5 - 3 1.0E-3 3 - 3.5 1.0E-3 3.5 - 6	Mortality risk relative (B...) 78.83 0 - 1 19.20 1 - 1.5 0.14 1.5 - 2 1.0E-3 2 - 2.5 1.0E-3 2.5 - 3 1.0E-3 3 - 3.5 1.0E-3 3.5 - 6
Mortality risk relative (Diet) 0.00 0 - 1 49.15 1 - 1.5 33.38 1.5 - 2 9.24 2 - 2.5 4.72 2.5 - 3 3.51 3 - 3.5	Mortality risk relative (Diet) 0.00 0 - 1 42.14 1 - 1.5 33.60 1.5 - 2 11.94 2 - 2.5 7.04 2.5 - 3 5.27 3 - 3.5
Dose of erythropoietin ... 12.63 0 - 1000 44.93 1000 - 6000 29.12 6000 - 11000 9.25 11000 - 16000 3.95 16000 - 21000 0.09 21000 - 26000 0.02 26000 - 31000 0.01 31000 - 36000 0.00 36000 - 41000	Dose of erythropoietin ... 2.97 0 - 1000 10.57 1000 - 6000 83.32 6000 - 11000 2.18 11000 - 16000 0.93 16000 - 21000 0.02 21000 - 26000 0.00 26000 - 31000 0.00 31000 - 36000 4.89E-4 36000 - 41000

Dose



Quality Report

Software Testing

Definitions

Unit number: The software development team that developed the software version

PM: The total number of person months used to develop and test the software version

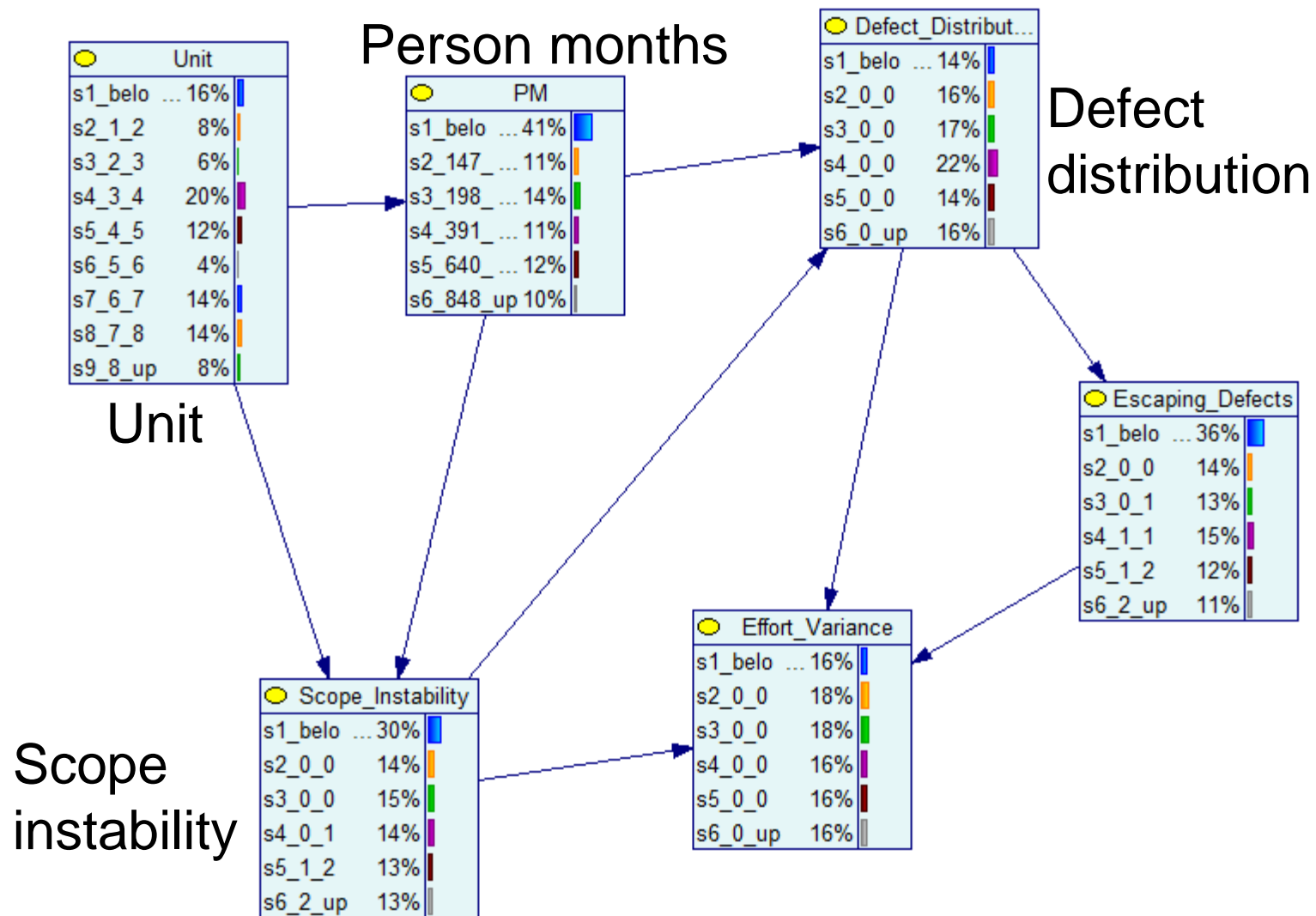
Escaping Defects: The number of Severity 1-3 defects detected during the first three months after release of software version divided by PM -the lower the better.

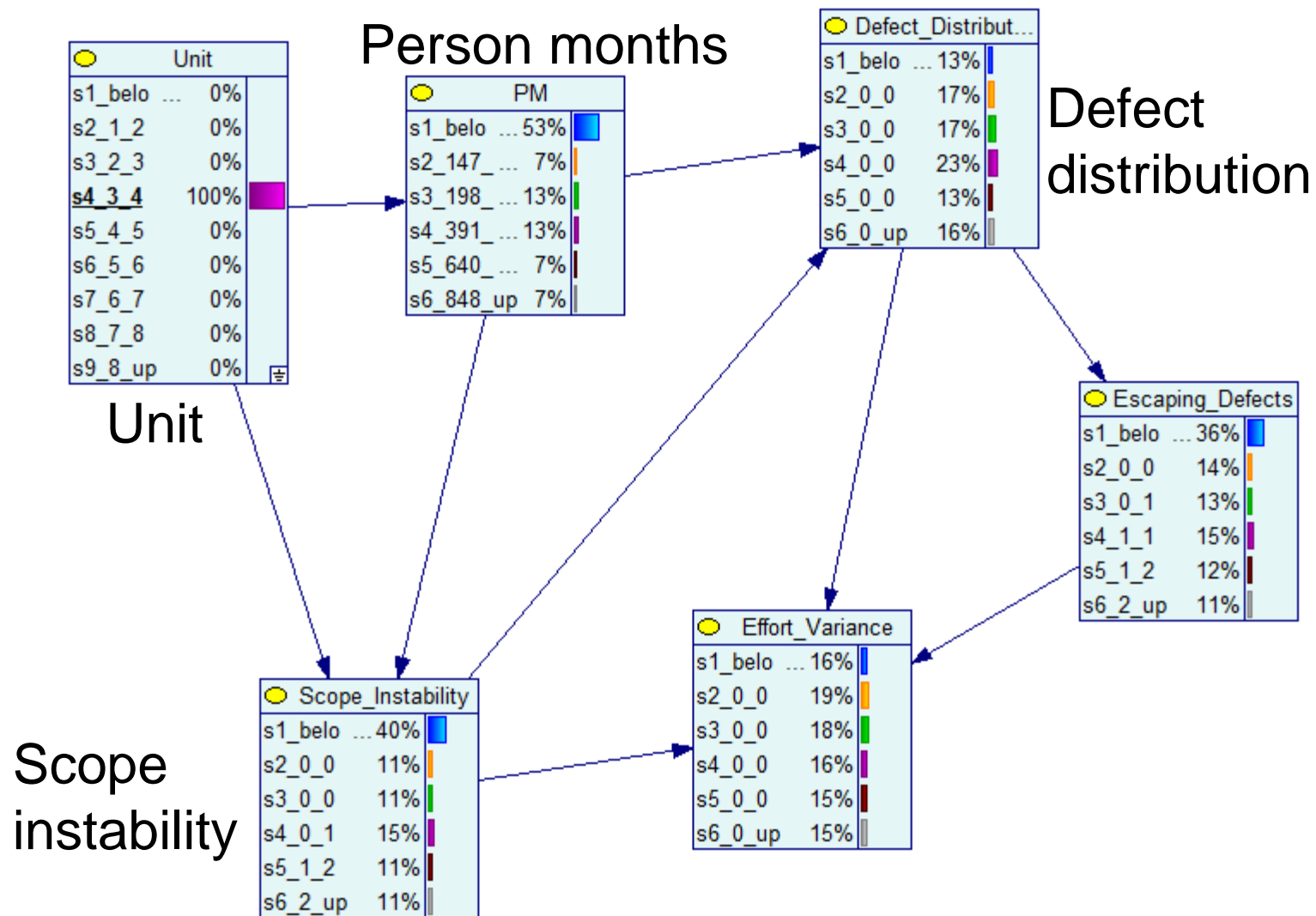
Defect Distribution: The proportion of defects detected during the various internal testing phases versus defects detected by customers during the first three months after release of software version -the higher the better.

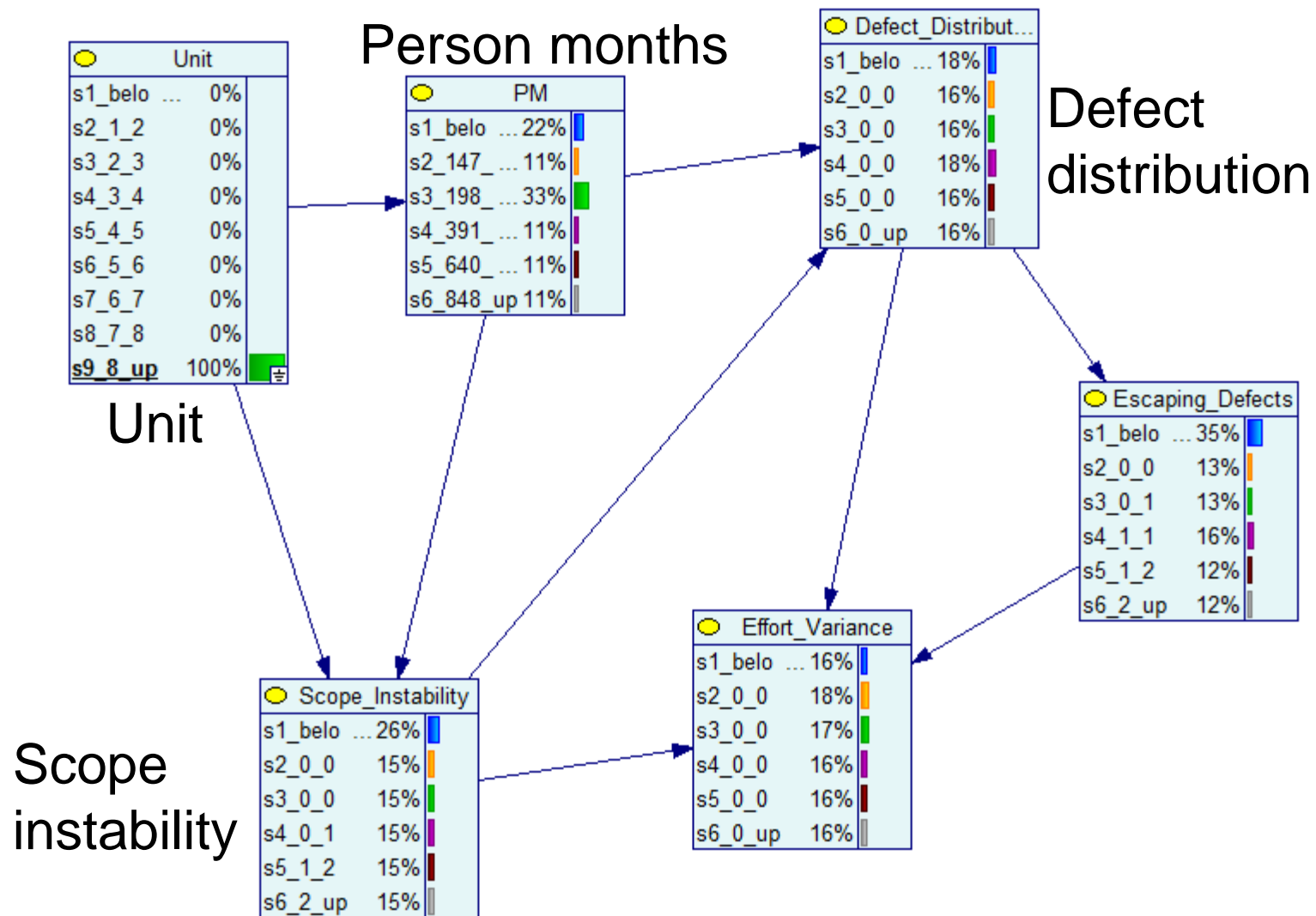
Effort Variance: The effort variance, in PM, from the budget baseline of the software version during the release development period

Scope Instability: Represents changes to requirements scoped to the release and stability of the software development baseline. i.e. number of changed, deleted and added requirements after scope sign-off date divided by the number of requirements in the release scope at release sign-off date.

Unit	PM	Escaping Defects	Defect Distribution	Effort Variance	Scope Instability
1.0	727	0.31	0.71	-0.03	0.01
1.0	250	1.63	0.37	-0.09	0.66
1.0	773	0.12	0.92	0.04	0.14
1.0	49	0.05	0.89	-0.07	0.14
1.0	52	0.23	0.74	-0.09	0.03
1.0	923	0.08	0.92	-0.04	0.00
1.0	21	1.27	0.52	0.11	0.00
2.0	7	0.43	0.76	0.00	0.00
2.0	60	0.20	0.61	0.05	0.05
2.0	105	0.40	0.74	0.02	0.15
3.0	747	0.60	0.53	0.31	0.80
3.0	25	1.87	0.57	0.09	0.21
4.0	230	1.27	0.16	0.36	0.00
4.0	553	3.31	0.14	0.92	0.00
4.0	57	0.93	0.66	0.06	0.20
4.0	29	0.75	0.58	-0.10	0.03
4.0	60	0.63	0.66	-0.18	0.73
4.0	16	0.06	0.92	-0.03	0.00
4.0	36	0.90	0.41	0.00	0.00
4.0	37	0.38	0.39	0.09	0.01
4.0	86	0.69	0.73	0.08	0.00
5.0	157	0.31	0.68	0.02	0.57
5.0	182	0.99	0.57	0.12	2.25
5.0	35	0.46	0.56	0.09	3.46

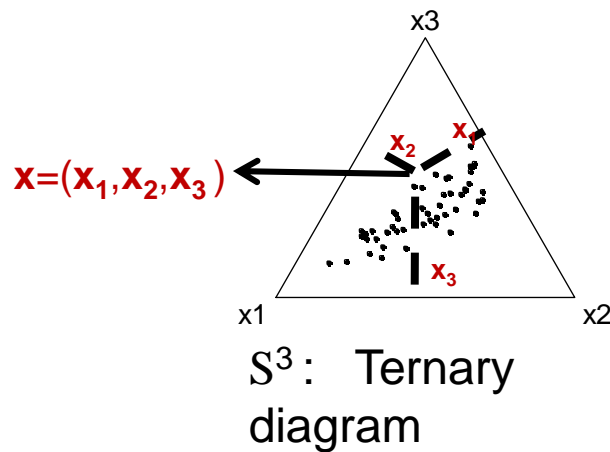






Compositional data (CoDa)

- CoDa: vectors of non-negative components showing the *relative importance of a set of **parts** in a total*.
- Sample space: the simplex
with $k = 1, 100, 10^6, 10^9$ (proportions, %, ppm, ppb) .
- The total “ k ”: is considered irrelevant, not informative.



$$S^D = \{\mathbf{x} \in \mathbb{R}_+^D : x_1 + x_2 + \dots + x_D = k\}$$

Two principles:

- *scale invariance* and
- *subcompositional coherence*



A four-hour workshop

Conference in honor of Corrado Gini
(Padua, 7-8 September, 2015)



Compositional Data (CoDa) methods in the analysis of customer surveys

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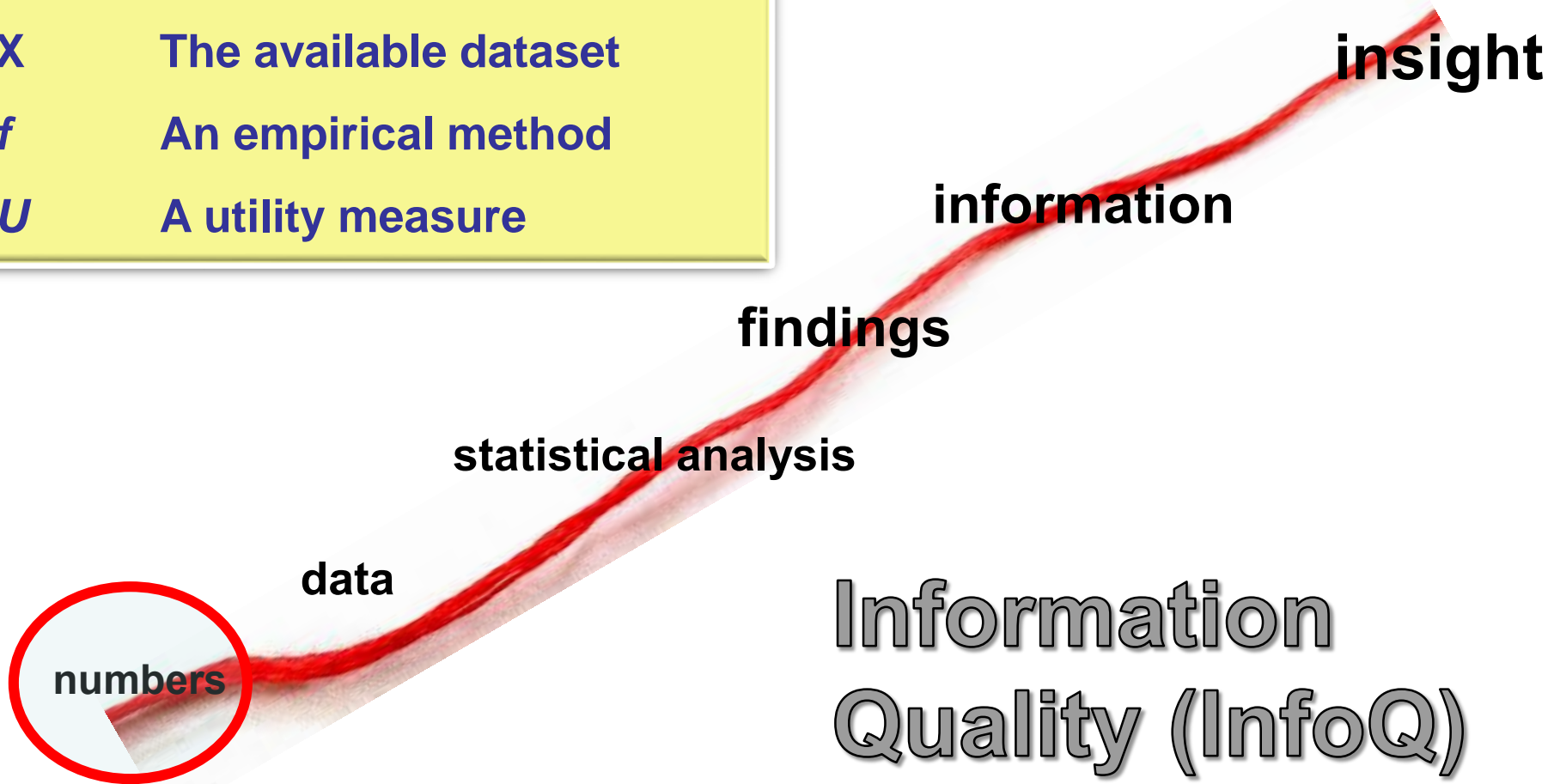
September 8th, 2015

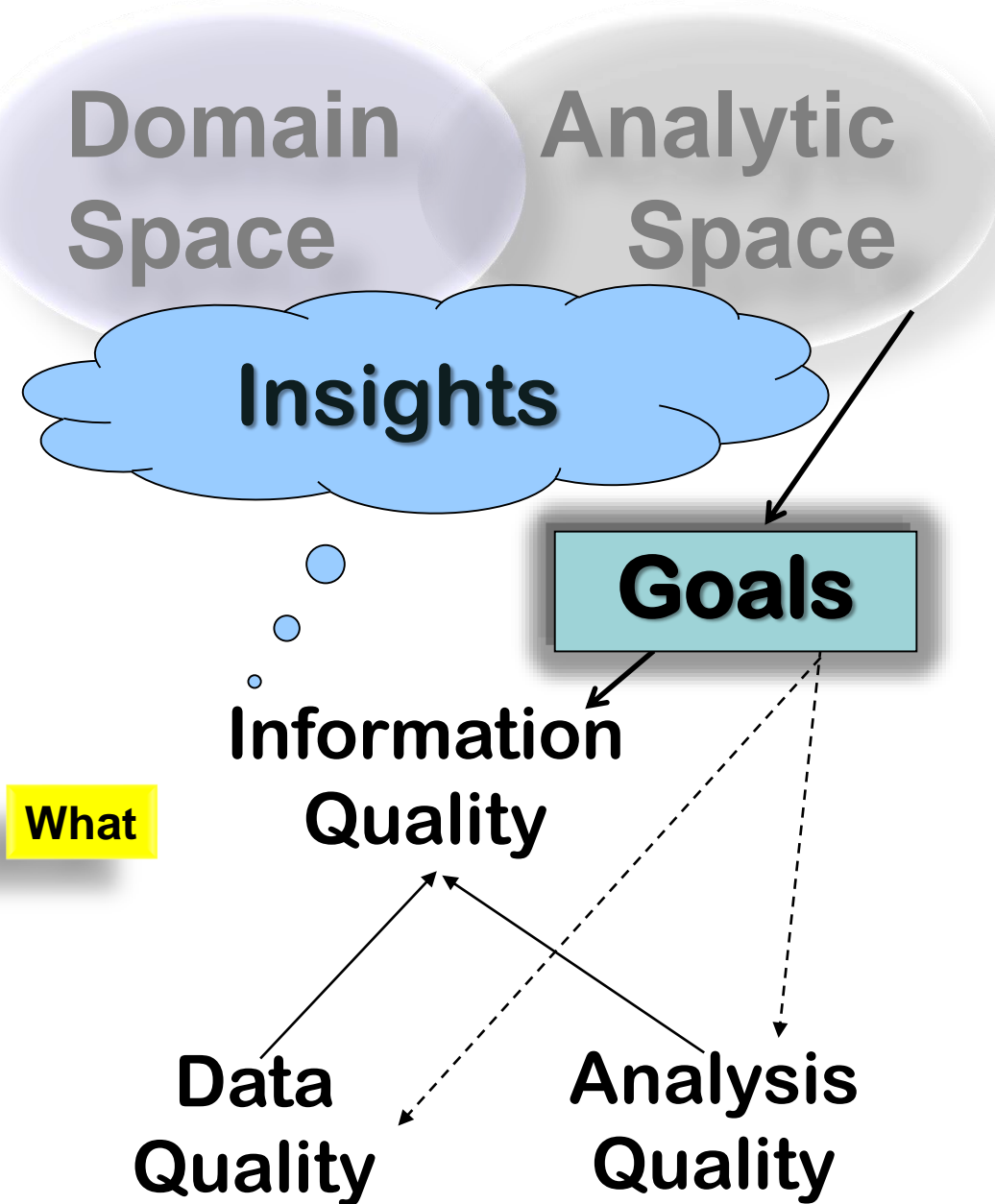
14:30-18:30

<http://convegnogini.stat.unipd.it/en/index.php#workshop>

$$\text{InfoQ}(f, X, g) = U(f(X|g))$$

g	A specific analysis goal
X	The available dataset
f	An empirical method
U	A utility measure





What

How

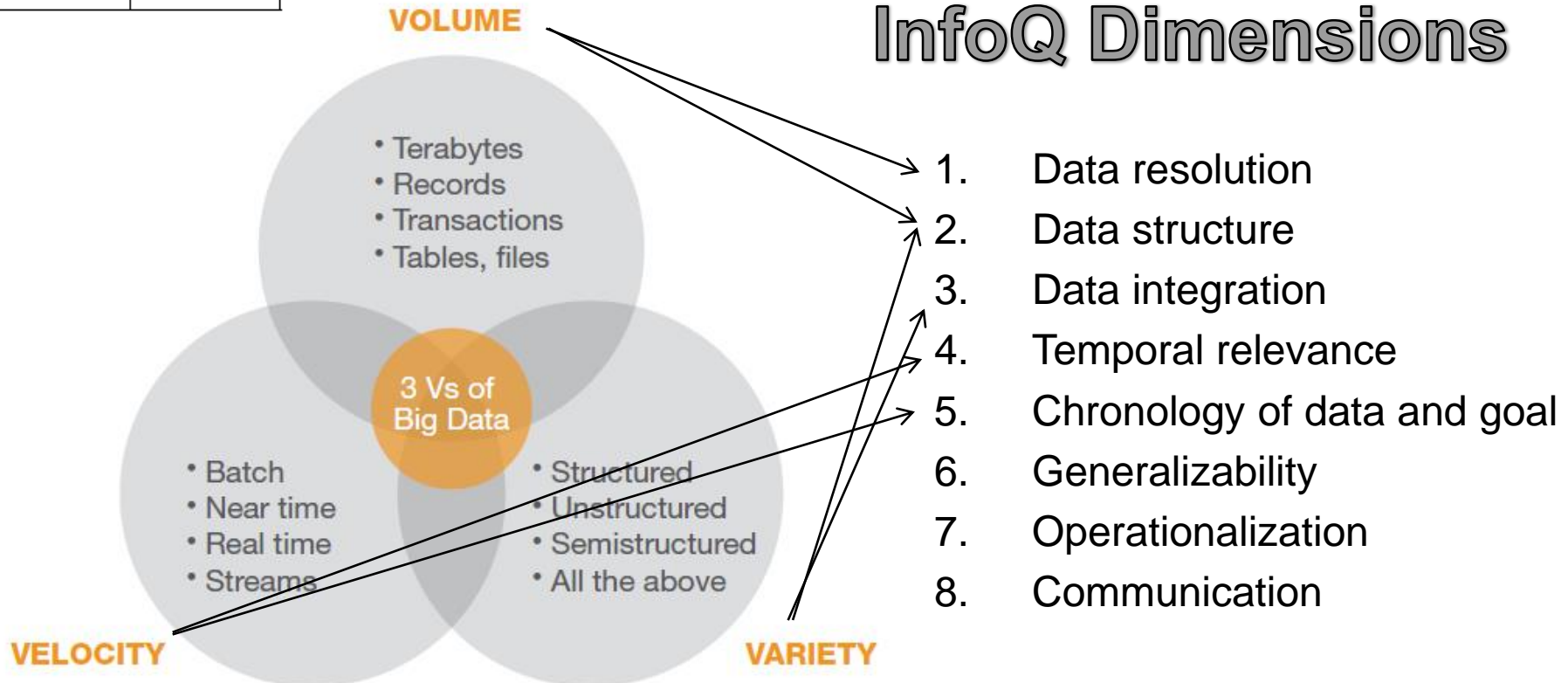
1. Data resolution
2. Data structure
3. Data integration
4. Temporal relevance
5. Chronology of data and goal
6. Generalizability
7. Operationalization
8. Communication

#	Dimension	Note	Value	Index
1	Data resolution		5	1.0000
2	Data structure		4	0.7500
3	Data integration		5	1.0000
4	Temporal relevance		5	1.0000
5	Generalizability		3	0.5000
6	Chronology of data and goal		5	1.0000
7	Concept operationalization		2	0.2500
8	Communication		3	0.5000
InfoQ Score = 0.68				

Power	Prefix
10^9	Giga
10^{12}	Tera
10^{15}	Peta
10^{18}	Exa
10^{21}	Zetta
10^{24}	Yotta

Big Data Analytics

InfoQ Dimensions



Why Bayesian Networks?

InfoQ Dimension	1 Mgmt	2 Web Usability	3 ICT Risks	4 Biotec	5 Surveys	6 Health	7 Testing	Dimension score
Data Resolution	1	4	5	4	5	4	4	3.50
Data Structure	2	3	5	4	4	5	4	3.71
Data Integration	3	4	4	4	4	5	5	4.09
Temporal Relevance	5	4	4	5	4	5	4	4.40
Chronology of Data and Goal	4	4	5	5	5	5	4	4.54
Generalizability	5	4	4	4	5	5	3	4.22
Operationalization	4	3	4	4	4	5	4	3.96
Communication	4	4	5	5	5	4	5	4.54
Use case InfoQ score	3.15	3.72	4.47	4.35	4.47	4.73	4.08	

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